Analyzing the turbulence in the Planetary Boundary Layer by the synergic use of remote sensing systems: Doppler wind lidar and aerosol elastic lidar" *by* Gregori de Arruda Moreira et al.

Author's response

We thank the anonymous reviewers for their comments, corrections and suggestions, which have helped to improve the quality of the manuscript. According to the referees' reports, the following changes have been performed on the original manuscript and a point-by-point response is included below.

Anonymous Referee #1

This manuscript presents results from the SLOPE campaign in Granada, Spain, in which the objective was to obtain closure between remote sensing and in-situ measurements. For this manuscript, the focus is on characterizing the planetary boundary layer using a Doppler lidar, multi-wavelength lidar (MULHACEN), and a profiling microwave radiometer, all operating at high temporal resolution (2 seconds). The authors investigate the use of fluctuations in aerosol number density from the elastic system (EL), vertical velocity fluctuations obtained from the Doppler lidar (DL), and potential temperature profiles retrieved from the microwave radiometer (MWR), to identify the boundary layer height (PBLH).

Some of the methodology is relevant, and the influence of random error introducing extra noise in higher-order moments is explored using suitable techniques, but the manuscript is not yet suitable for publication unless some major issues are addressed.

Major comments

The manuscript title and abstract suggests that different methods to determine PBLH will be combined synergistically, but this is not discussed at all in the main text. The main text seems to focus on whether various parameters derived from each instrument agree and does not suggest how they can be combined. In addition, the reader is not informed how PBLH should be derived from many of the DL and EL parameters, or how they could be combined if the purpose was to describe a synergistic retrieval method. Please decide whether you are describing a synergistic approach, or an intercomparison, and structure the manuscript accordingly.

We thank the Reviewer 1 for these comments. Such comments are in agreement with Referee#2, and have been accordingly addressed in section "Anonymous reviewer#2 - Major issue 1". Thus, we would like to remark that the objective of this work is not to compare the PBLH retrievals from different instrument because it has been demonstrated in previous articles (e.g. Bravo-Aranda et al, 2017; Moreira et al., 2018a) that instruments and techniques based on different tracers and observed quantities retrieve the height of different PBL sublayers. In this way, we propose here to use in a synergic way the information on the PBL obtained by these different remote sensing techniques in order to get a better understanding on the evolution of the PBL.

The EL and DL parameters are calculated over 1-hour periods. Is this 1-hour timescale suitable during rapidly varying conditions such as during the morning growth of the boundary layer? Did you try using a running average? What is the impact if you change the averaging period, and why was 1-hour chosen when the MWR data are averaged over 30 minutes?

We thank the Reviewer 1 for this comment. We performed some tests with smaller time scales, such as 30 and 45 minutes. However, the influence of noise is larger and the obtained values of the integral time scale are lower. As we argued previously, here we do not do a comparison among MWR and the other remote sensing systems retrievals and, therefore, the different time scale does not interfere in our analysis.

The manuscript requires a much more rigorous description of the processes driving turbulent mixing in the boundary layer. This does not need to be very long, but any processes referred to should be described accurately, e.g. it is the positive surface heat flux that is responsible for buoyancy (convection), not just intensifying convection. The energy flux balance at the surface partitions net radiation into sensible heat flux, latent heat flux and ground heat flux, hence, there can still be a positive sensible heat flux even when the net radiation is negative, such as during the early evening in urban regions, which is almost certainly what is happening in the two case studies shown here. It is not surprising that RH is somewhat inversely correlated with temperature if the specific humidity mixing ratio remains constant; however it is not safe (and not necessary) to state anything about latent heat fluxes if you are not measuring them.

We thank the Reviewer 1 for the comments. In order to clarify this point, the text has been changed as follows:

(Page 8, Line 272)

"This process is in agreement with the behavior of skewness of w' ($\boldsymbol{S_{w'}}$) shown in Figure 8-C. $\boldsymbol{S_{w'}}$ is directly associated with the direction of turbulent movements. Thus, positive values correspond with a surface-heating-driven boundary layer, while negative ones are associated to cloud-top long-wave radiative cooling. If $\boldsymbol{S_{w'}}$ is positive, both $\boldsymbol{\sigma^2_{w'}}$ and TKE (Turbulent Kinetic Energy) are being transported upwards and, consequently, the red regions in Figure 13-C represent positive values of $\boldsymbol{S_{w'}}$ and the blue regions refer to negative ones. During the stable period, there is predominance of low values of $\boldsymbol{S_{w'}}$. Nevertheless, as air temperature increases (transition from stable to unstable period), $\boldsymbol{S_{w'}}$ values begin to become positive and increase with the ascent of the $PBLH_{MWR}$ (CBL). Air temperature begins to decrease around 18:00 UTC, causing the reduction of $\boldsymbol{S_{w'}}$. In this moment the transition from unstable to stable period occurs and, therefore, the reduction in $PBLH_{MWR}$ is due to the $SBLH detection$.

Figure 8-D shows the values of net surface radiation (R_n) that are estimated from solar global irradiance values using the seasonal model described in Alados et al. (2003). The negative values of R_n are concentrated in the stable region. R_n begins to increase around 06:00 UTC and reaches its maximum in the middle of the day. Comparing figures 8-C and 8-D, we can observe similarity among the behavior of $\boldsymbol{S_{w'}}$, R_n and surface air temperature, because these variables increase and decrease together, as expected.

The increase of R_n causes the rise of surface air temperature, which contributes to the positive latent heat flux from the surface ($S_{w'}$) and, consequently, the growth of the $PBLH_{MWR}$ (CBL). R_n begins to decrease certain time before the other variables, but the intense reduction of air temperature and decrease of $S_{w'}$ and SBLH detection occurs when R_n becomes negative again, although there can still be a positive sensible heat flux, what is characteristic of early evening in urban regions due to the release of the ground heat flux at that time.

Figure 8-E presents the values of surface air temperature and surface relative humidity (RH). Air surface temperature is directly related with R_n and $S_{w'}$ values, as afore mentioned and expected. On the other hand, RH is inversely correlated with temperature and, thus, with the rest of variables, due to the relative constancy of the water vapor mixing ratio characteristic of our site during the study."

Minor comments

MWR data analysis: The MWR retrievals have, by some margin, the lowest vertical resolution of the methods detailed here, especially at the altitudes for typical daytime PBLH. The PBLH retrievals also seem very smooth in time. How does this compare with PBLH retrievals from DL and EL? Is it likely that the MWR provides the most accurate measure of PBLH? Do you use MWR PBLH as a reference for DL and EL retrievals or not? The manuscript requires some discussion on these issues.

We thank the Reviewer 1 for this comment. As aforementioned, in this paper we do not aim to perform a comparison of PBLH obtained from different method or instruments. This is something that we did in a previous paper: de Arruda Moreira et al. (2018a).

We use the MWR data as reference to estimate the PBLH due to a comparison between MWR and radiosonde data performed during a 3-month campaign in Granada-Spain (Moreira et al., 2018a). This comparison demonstrated a good correlation between these instruments in stable and convective situations.

In order to clarify this point, the text has been changed as follows:

(Page 5, line 152)

"This methodology of PBLH detection was selected as the reference due to the results obtained during a performed campaign of comparison between MWR and radiosonde data, where twenty-three radiosondes were launched. High correlations were found between PBLH retrievals provided by both instruments in stable and unstable cases. Further details are given by Moreira et al. (2018a)."

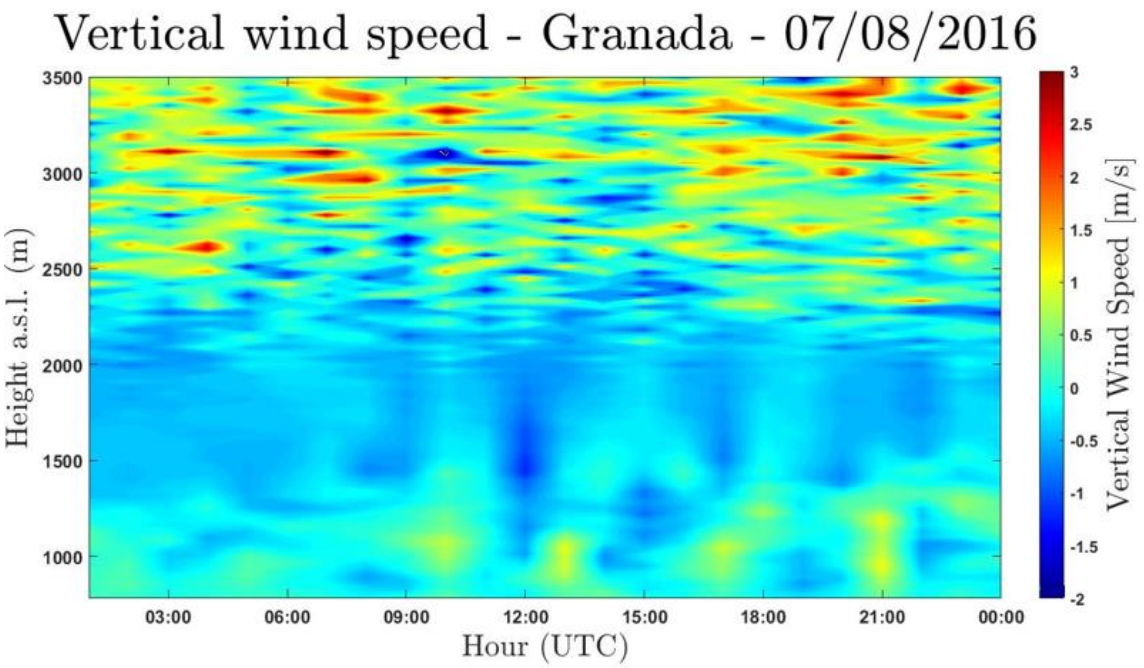
Doppler lidar analysis: There are no time-height plots of the DL signal and velocity measurements so it is difficult to judge whether some of the features seen in the DL parameters are due to low SNR conditions. The interpretation of skewness is not appropriate and should be rewritten.

We thank the Reviewer 1 for the comments. In order to clarify this point, the text has been changed as follows:

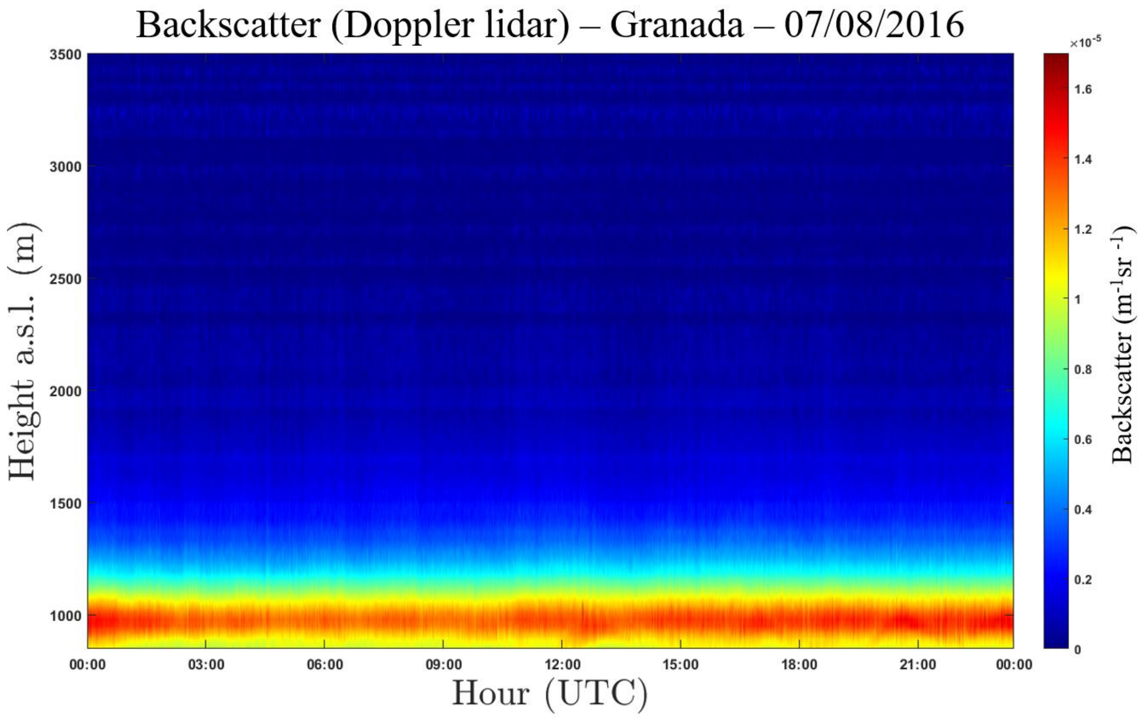
(Page 8, Line 272)

"This process is in agreement with the behavior of skewness of w′ ($\boldsymbol{S_{w'}}$) shown in Figure 8-C. $\boldsymbol{S_{w'}}$ is directly associated with the direction of turbulent movements. Thus, positive values correspond with a surface-heating-driven boundary layer while negative ones are associated to cloud-top long-wave radiative cooling. If $\boldsymbol{S_{w'}}$ is positive, both $\boldsymbol{\sigma^2_{w'}}$ and TKE (Turbulent Kinetic Energy) are being transported upwards and consequently, the red regions in Figure 13-C represent positive values of $\boldsymbol{S_{w'}}$ and the blue regions refer to negative ones."

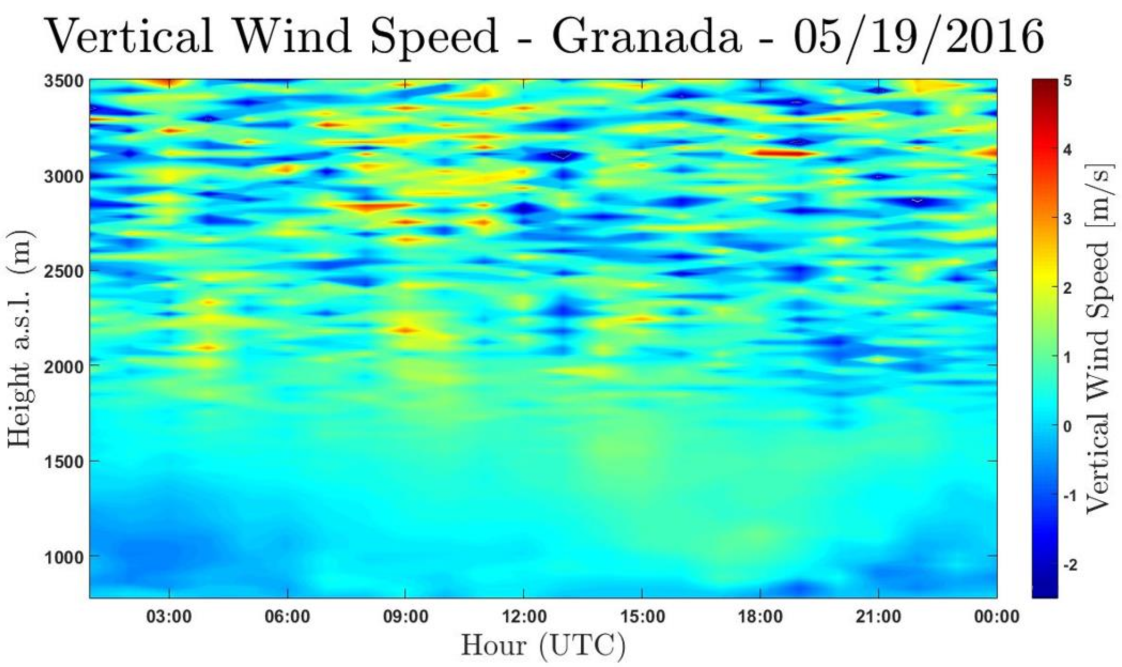
In addition, the following figures will be provided as supplementary materials:



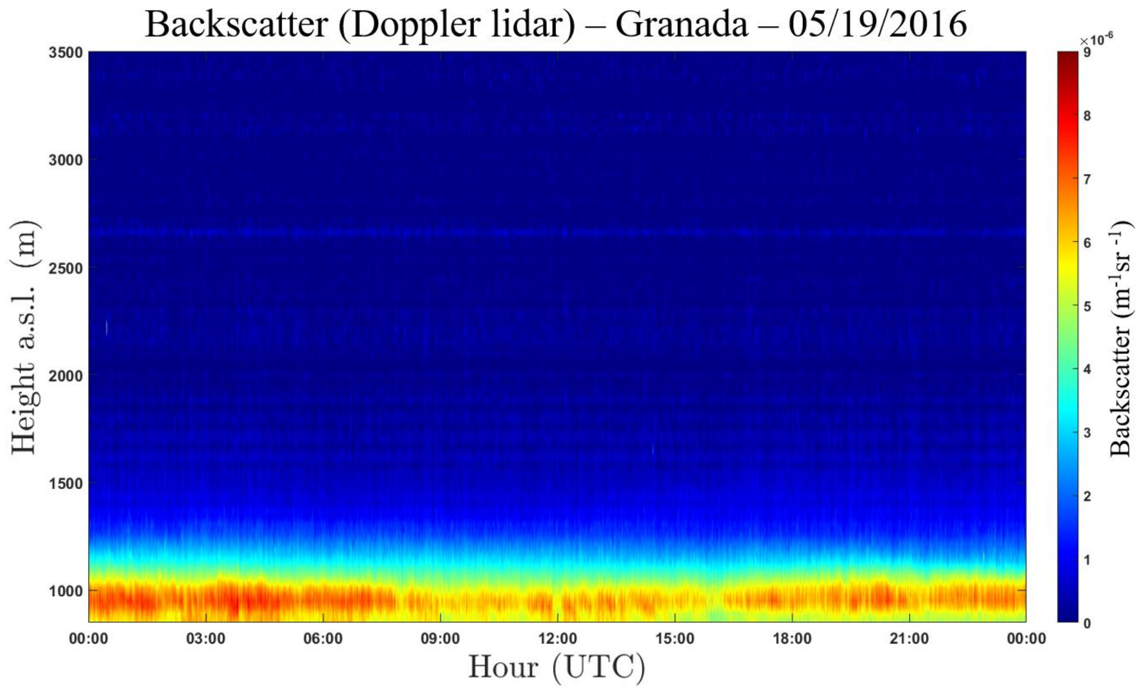
Supplementary Material – Figure 1



Supplementary Material – Figure 2



Supplementary Material – Figure 3



Supplementary Material – Figure 4

Elastic lidar analysis: Is it safe to assume the two-way transmittance is negligible? Especially since you use the 532 nm wavelength (molecular extinction may be important). What are the typical molecular, aerosol and total extinction values for the cases shown here?

Yes. In order to clarify this point, the text has been changed as follows:

(Page 9, Line 300)

"The period between 13:00 and 14:00 UTC has been selected to be analyzed. Figure 10-A presents the profiles of molecular ($\beta_{Molecular}$) and aerosol ($\beta_{Aerosol}$) backscatter coefficients at 532 nm. Although β_{532} is composed by $\beta_{Molecular}$ and $\beta_{Aerosol}$, it is possible to observe the predominance of $\beta_{Aerosol}$ in the region below of the $PBLH_{MWR}$, as demonstrated in figure 10-B by the β_{Ratio} profile . *Similar results were demonstrated by Moreira et al. (2018b), therefore reinforcing the viability of the use of this wavelength in studies about turbulence."*

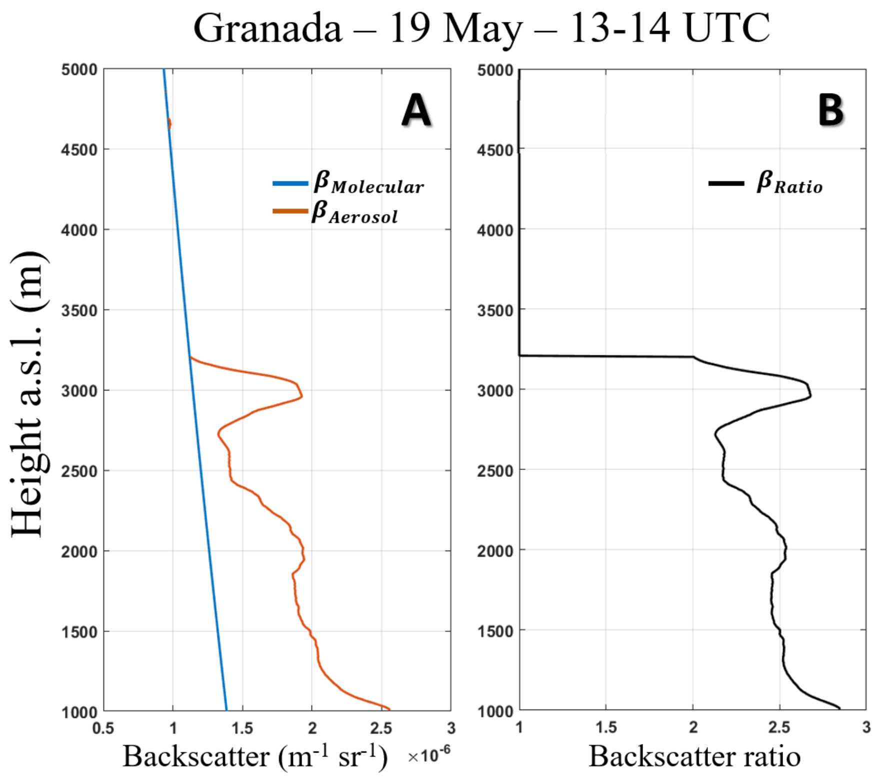


Figure 10 – (A) $\beta_{Molecular}$ (blue line) and $\beta_{Aerosol}$ (orange line). (B) β_{Ratio} (black line). All profiles were obtained from the 532 nm lidar signal

(Page 11, Line 357)

"Figure 14-A presents the $\beta_{Molecular}$ and $\beta_{Aerosol}$ profiles, similarly to figure 10-A. It is evident the predominance of $\beta_{Aerosol}$ in the region below $PBLH_{MWR}$, as demonstrated by β_{Ratio} profile in figure 14-B. However due to presence of dust layer this dominance of $\beta_{Aerosol}$is extended to approximately 4500 m a.s.l. Therefore the methodology proposed by Moreira et al. (2018b), based on considerations of Pal et al. (2010), can be applied."

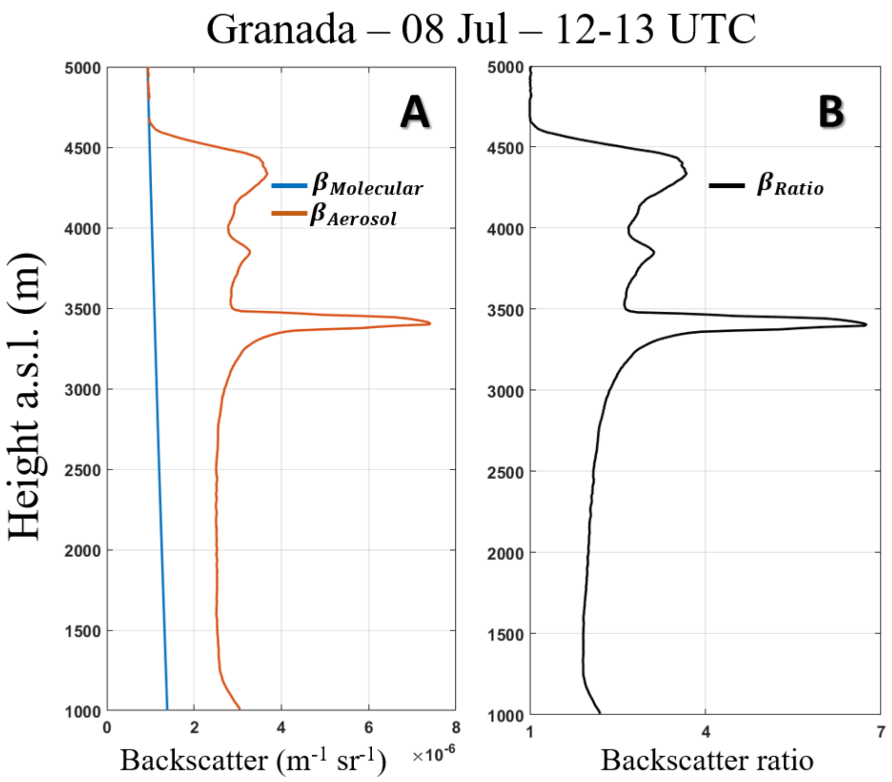
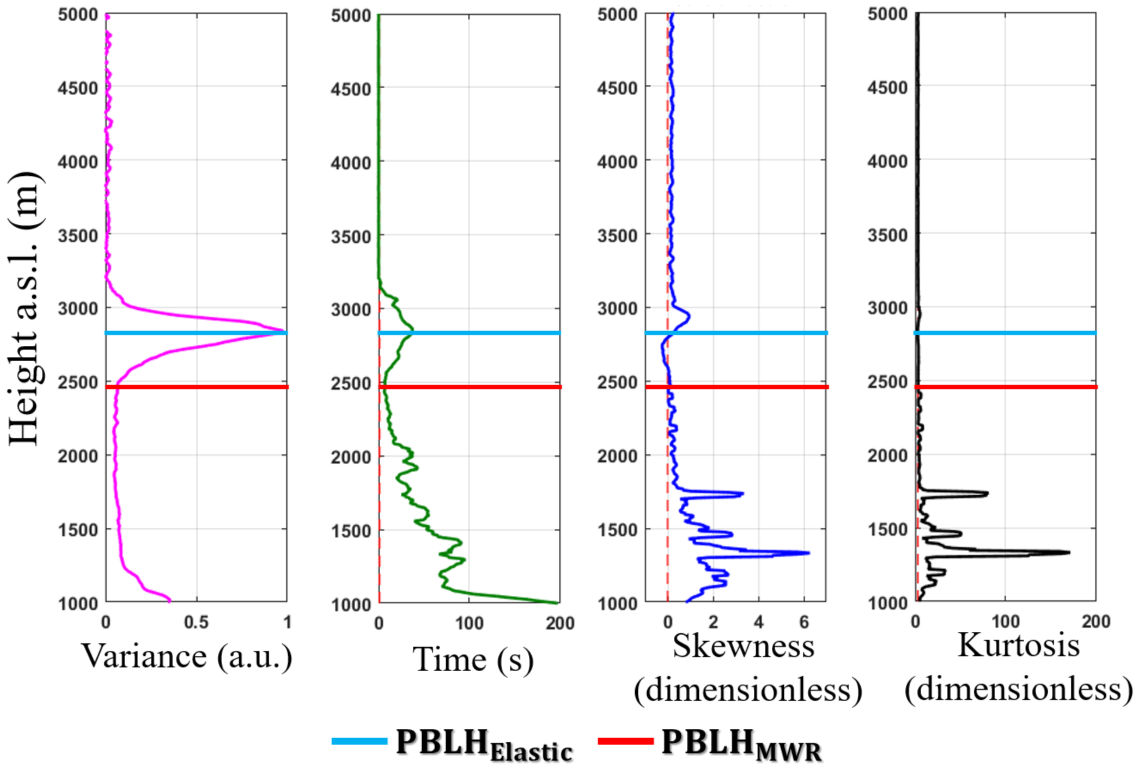


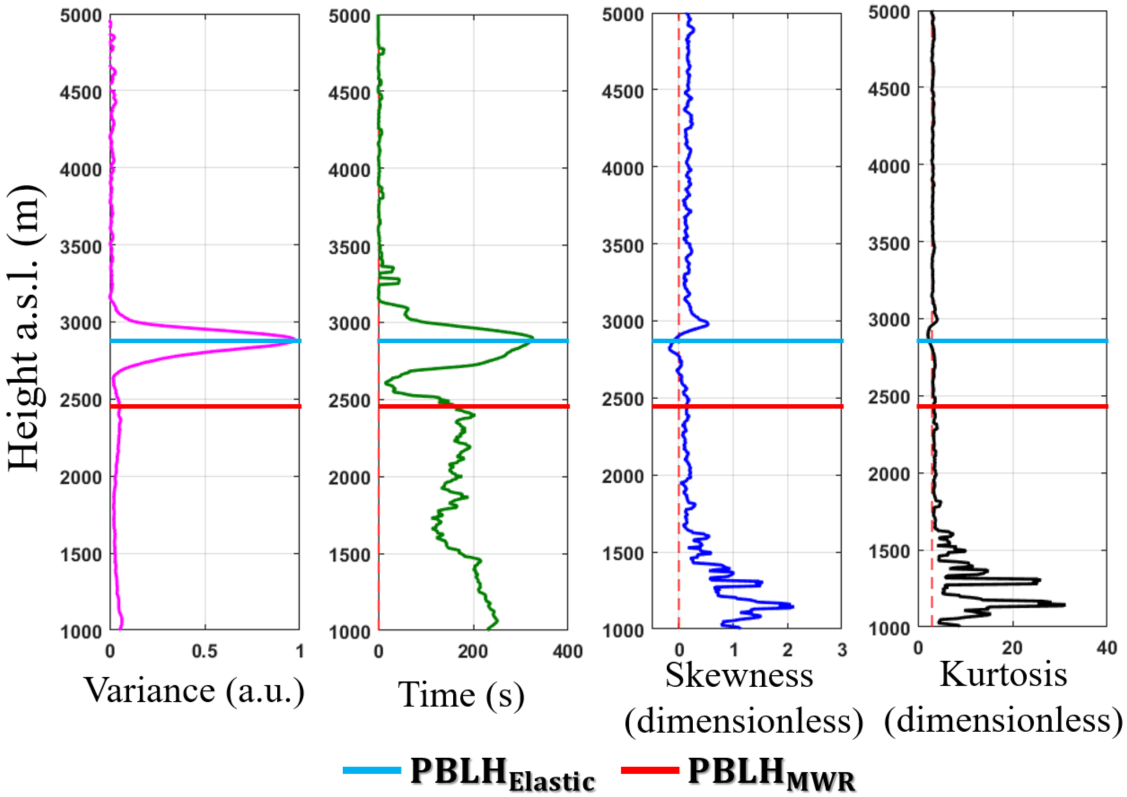
Figure 14 – (A) $\beta_{Molecular}$ (blue line) and $\beta_{Aerosol}$ (orange line). (B) β_{Ratio} (black line). All profiles were obtained from the 532 nm lidar signal

There are no time-height plots of the statistical parameters calculated from EL data so it is difficult to judge whether these provide a reliable guide to the boundary layer development - please include these.

We thank the Reviewer 1 for the comments. In order to clarify this point, we have been added two figures in supplementary material, which demonstrate that all profiles maintain theirs specific behavior, as commented in page 9 – line 310, during the PBLH evolution.



Supplementary Material - Figure 5 - Statistical moments obtained from elastic lidar data at 14 to 15 UTC - 19 May 2016. From left to right: variance [$\sigma^2_{RCS'}$], integral time scale [$\tau_{RCS'}$], skewness [$S_{RCS'}$] and kurtosis [$K_{RCS'}$].



Supplementary Material - Figure 6 - Statistical moments obtained from elastic lidar data at 15 to 16 UTC - 19 May 2016. From left to right: variance [$\sigma^2_{RCS'}$], integral time scale [$\tau_{RCS'}$], skewness [$S_{RCS'}$] and kurtosis [$K_{RCS'}$].

Doppler lidar and Elastic lidar analysis: Since you make some effort to quantify the influence of noise on the statistical parameters derived from these two systems, it would be beneficial to *discuss how this impacts your interpretation*, e.g include time-height plots of the correction factor or relative correction, relative importance in determining PBLH, how much temporal averaging is required to obtain good results.

We thank the reviewer 1 for this comment, but as aforementioned in this paper we do not have as objective the PBLH detection for different remote sensing systems. In previous articles (e.g. Bravo-Aranda et al, 2017; Moreira et al., 2018a) we performed a comparison between the PBLH obtained from different remote sensing systems (MWR,Elastic lidar and Doppler lidar), as well as, a discussion about which factors can influence the PBLH generated from data of these systems.

What is the minimum integral time scale that the DL and EL can measure? Is it the acquisition time that allows you to observe turbulence throught the PBL, or is it more likely to be a function of the instrument sensitivities?

The integral time scale (the minimum time where turbulent events are connected) has a minimum acceptable value coincident with the acquisition time of each system (Pal et al., 2010). Thus, in our case the nominal acquisition time is 1 s for the elastic lidar, but we use 2 s for both elastic and Doppler lidar because higher temporal resolutions do not allow for observing turbulence with our instruments. More sensitive systems have lower minimum time, e.g. High Spectral Resolution Lidar utilized by McNicholas et al. (2014).

Case study 2: Did you try cloud-screening EL data before calculating EL parameters? The PBLH from EL would agree much better with PBLH from MWR in Figure 13, and maybe Figure 14 (it is hard to tell with the scales used). Clouds should also be visible in DL data.

We thank the reviewer 1 for this comment. No, any cloud-screening method was not applied before calculating the EL parameters due to the main objective of this manuscript is not to improve the quality of PBLH detection from EL data, but to show how clouds and Saharan dust layers can influence in the PBL characterization when aerosols are used as tracers.

Technical comments

Line 36: What do you mean by cyclic processes?

Line 37: Large variability of what?

We thank the Reviewer 1 for these two questions. In order to clarify these points, the text has been changed as follows:

(Page 1, Line 36)

"...is mainly characterized by turbulent processes and a daily evolution cycle..."

Line 39: Surface heating is unlikely to impact the upper troposphere.

We thank the Reviewer 1 for this comment. In order to clarify this point, the text has been changed as follows:

(Page 1, Line 40)

"This process intensifies the convection and, thus, the ascending warm air masses heat the air masses situated in the upper regions of troposphere, originating the Convective Boundary Layer…"

Line 84: Distinct?

We thank the Reviewer 1 for this question. In order to clarify this point, the text has been changed as follows:

(Page 3, Line 85)

"…operating at different altitudes…"

Line 89: Replace 'responsible of ' with 'responsible for'.

Done.

Line 98: Explain '(s and p)'.

Our elastic lidar is polarization-sensitive. In this way, "s" and "p" refers to the parallel channel (p) and the perpendicular one (s). The text has been changed accordingly:

(Page 3, Line 99)

"…532 (parallel and perpendicular polarization)…"

Line 104: Please include a few more Doppler lidar operating parameters: pulse repetition frequency, telescope focus.

We thank the Reviewer 1 for this comment. In order to clarify this point, the text has been changed as follows:

(Page 3, Line 106)

"It operates at 1.5 µm with pulse energy and repetition rate of 100 µJ and 15 KHz, respectively. This system record the backscattered signal with 300 gates, being the range gate length is 30 m, with the first gate at 60 m. The telescope focus is set to approximately 800 m."

Line 106: Use 'laser beam pointing at vertical', since the ground surface may not be horizontal!

We thank the Reviewer 1 for this comment. In order to clarify this point, the text has been changed as follows:

(Page 3, Line 109)

"...laser beam is pointed at vertical with respect..."

Line 108: Replace 'which is part of the MWRNet' with 'which is a member of MWRNet'.

Done.

Line 112: State how many frequencies measured in each band.

We thank the Reviewer 1 for this comment. In order to clarify this point, the text has been changed as follows:

(Page 4, Line 127)

"K-band (water vapor – frequencies: 22.24 GHz, 23.04 GHz, 23.84 GHz, 25.44 GHz, 26.24 GHz, 27.84 GHz, 31.4 GHz) and V-band (oxygen – frequencies: 51.26 GHz, 52.28 GHz, 53.86 GHz, 54.94 GHz, 56.66 GHz, 57.3 GHz, 58.0 GHz)"

Line 128: Replace 'MWR data analyzes' with 'MWR data analysis'

Done.

Line 130: PBLH not defined yet.

We thank the Reviewer 1 for the comments. In order to clarify this point, the text has been changed as follows:

(Page 4, Line 131)

"...PBL Height ($PBLH_{MWR}$)..."

Line 188: Do you mean '(Pal et al., 2010)'?

Yes, the manuscript has been modify accordingly:

(Page 6, Line 192)

"...(Pal et al., 2010)..."

Line 220: Replace ’Under’ with ’Below’.

Done.

Lines 220-221: This sentence does not make sense. Do you mean ’Below the PBLH_MWR, correcting for noise does not have a significant impact on the profile, but is more evident above’?

We thank the Reviewer 1 for this question and we apologize for this mistake. In order to clarify this point, the text has been changed as follows:

(Page 7, Line 239)

“The profiles corrected by -2/3 law do not present notable differences in comparison to uncorrected profiles. On the other hand, the profiles corrected by the first lag correction have significant differences below the $PBLH_{MWR}$, mainly the $\boldsymbol{\sigma_{w'}^2}$ *(*$\boldsymbol{S_{w'}}$ *only in the first 50 m**)**, and some slight differences are evident above $PBLH_{MWR}$.”*

Line 261: Define Rn (presumably net surface radiation).

Done:

(Page 8, Line 266)

“…net surface radiation (R_n)…”

Line 320: Do you mean ’(Ansmann, 2010)’?

Yes, we do and the text has been changed as follows:

(Page 10, Line 325)

“…(Ansmann et al., 2010)…”

Figure 4: Autocovariance from DL? What are the units for variance and skewness?

Figures 5,7: Profiles from which instrument, and from which location? At what time, and on what day? What height is the surface?

Figure 6: Autocovariance from EL? What are the units for variance, skewness and kurtosis?

We thank the Reviewer 1 for these questions. In order to clarify these points, the figures has been changed as follows:

In figure 4 the title has been changed of "Autocovariance" to "Autocovariance function of w'"

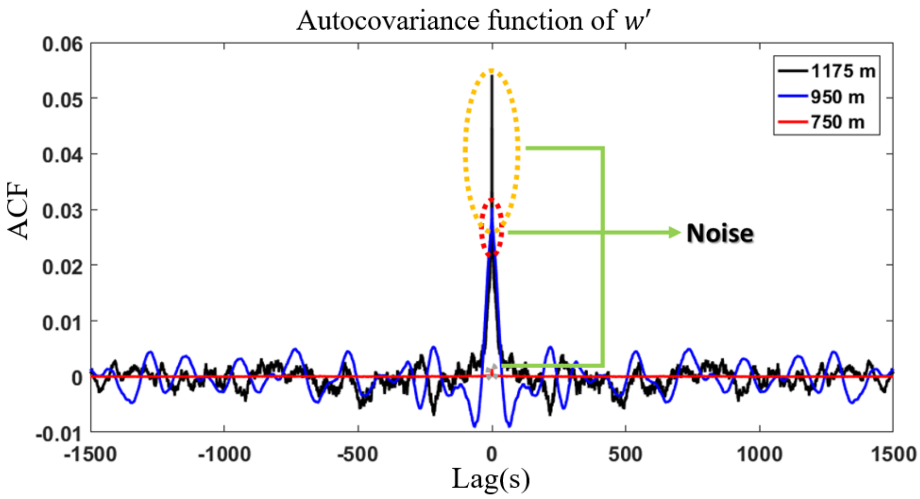


Figure 4 – Autocovariance function (ACF) of w' at three different heights

In figure 5 the units of Variance (m/s²) and Skewness (a.u.) have been added, as well as, information about time, location of measurement.

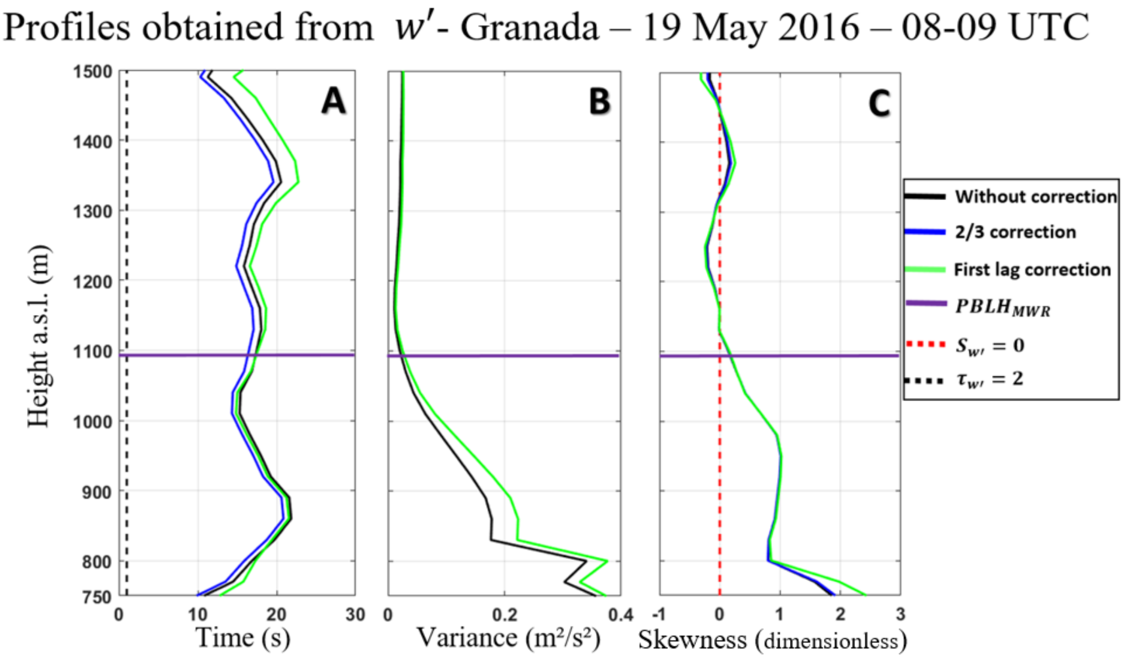


Figure 5 – A - Vertical profile of Integral time scale ($\tau_{w'}$). B - Vertical profile of variance ($\sigma^2_{w'}$). C - Vertical profile of Skewness. ($S_{w'}$)

In figure 6 the title has been changed of "Autocovariance" to "Autocovariance function of RCS'"

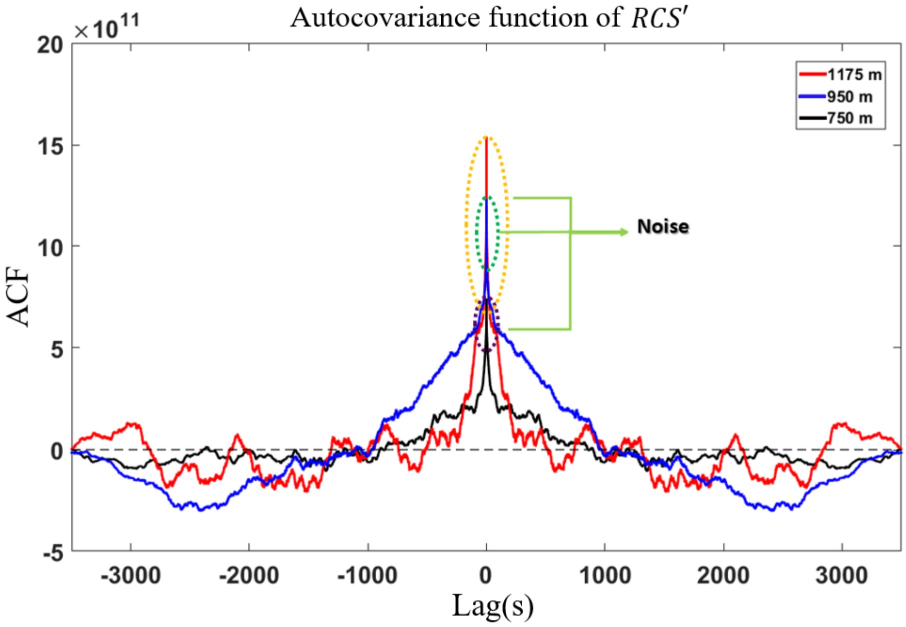


Figure 6 – Autocovariance of RCS' to three different heights

In figure 7 the units of Variance (m^2/s^2), Skewness (a.u.) and Kurtosis (a.u.) have been added, as well as, information about time, location of measurement.

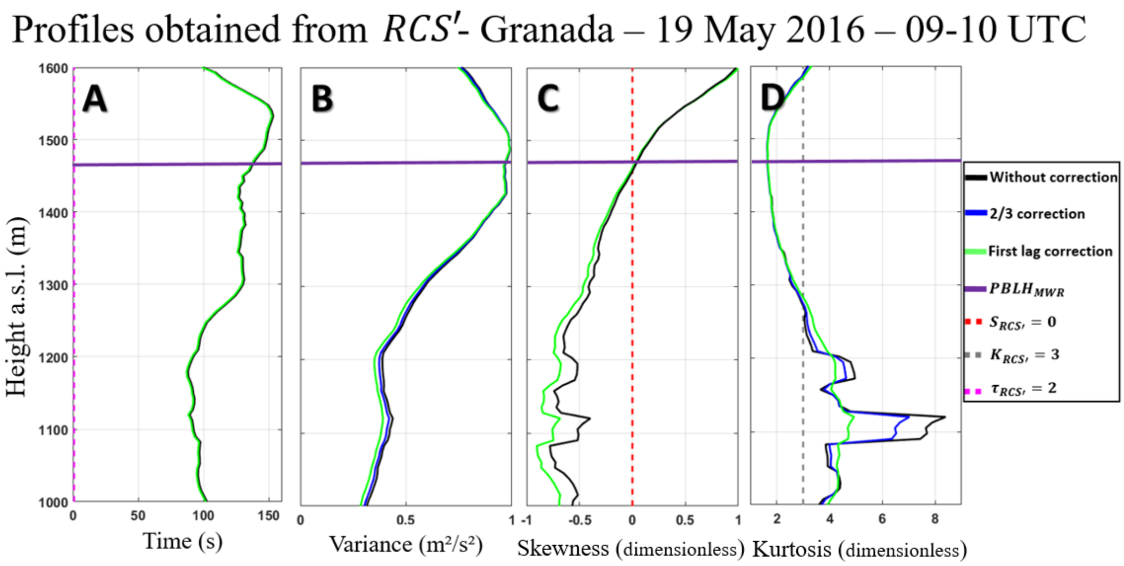


Figure 7 – A- Vertical profile of Integral time scale ($\tau_{RCS'}$). B - Vertical profile of variance ($\sigma^2_{RCS'}$). C - Vertical profile of Skewness ($S_{RCS'}$). D - Vertical profile of Kurtosis ($K_{RCS'}$).

Figures 8,11: Which instrument are panels A-C from? Are the black lines (temperature) from the MWR retrieval? Is it more appropriate to plot variance in log scale?

We thank the Reviewer 1 for these questions. In order to clarify these points, the figures has been changed as follows:

In figure 8-A, B and C a label has been added.

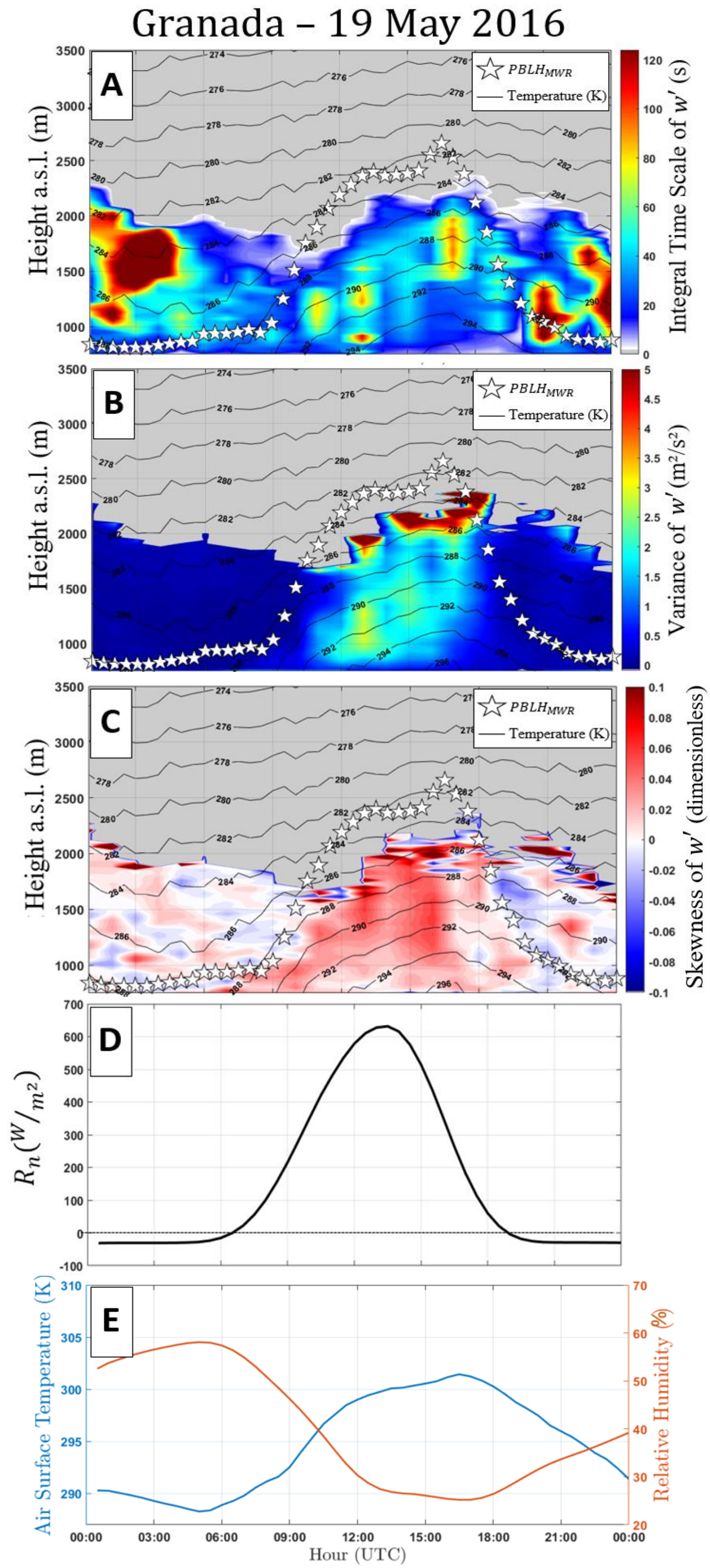


Figure 8 – A – integral time scale [$\boldsymbol{\tau_{w'}}$], B – variance [$\boldsymbol{\sigma}^2_{w'}$], C – skewness [$\boldsymbol{S_{w'}}$], D – net radiation [$R_n$], E – Air surface temperature [blue line] and surface relative humidity [RH – orange line]. In A, B and C black lines and white stars represent air temperature and $PBLH_{MWR}$, respectively.

In figure 12-A, B and C a label has been added.

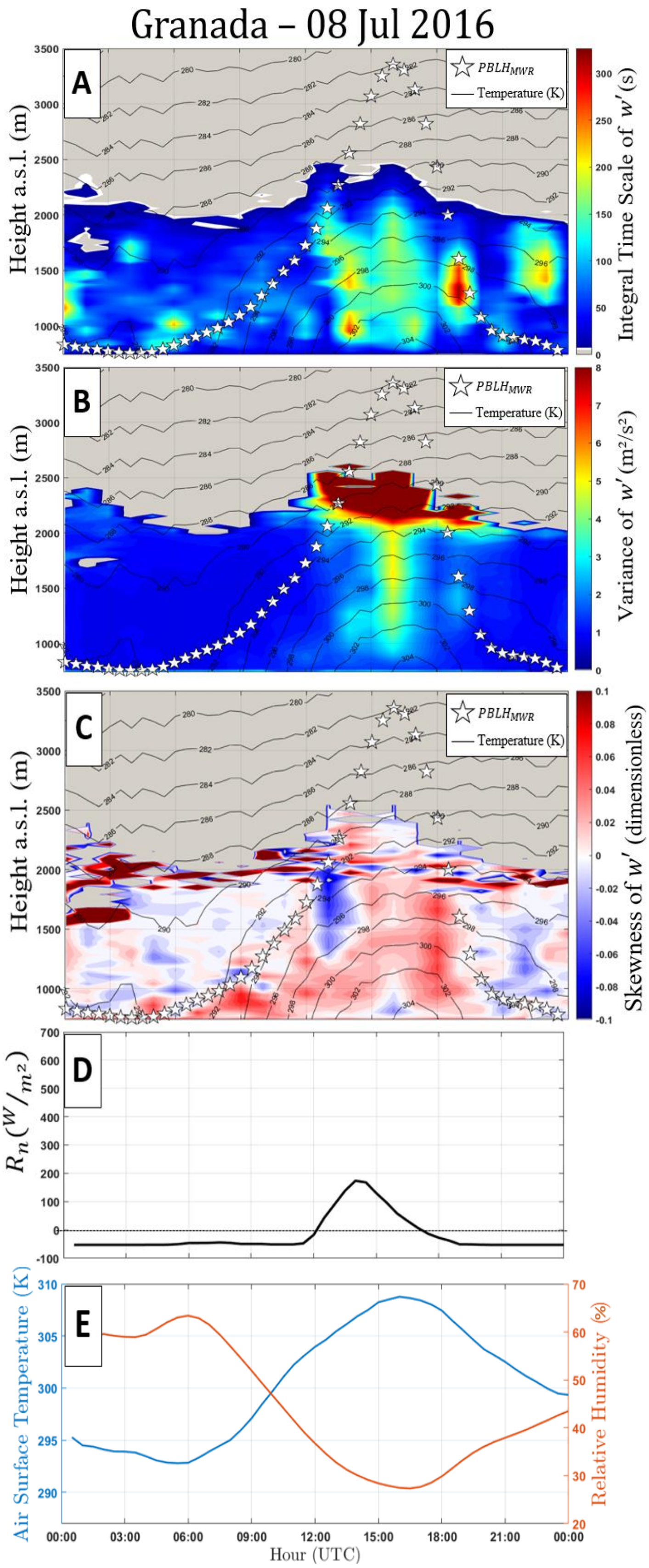


Figure 12 - A – integral time scale [$\boldsymbol{\tau_{w'}}$], B – variance [$\boldsymbol{\sigma^2_{w'}}$], C – skewness [$\boldsymbol{S_{w'}}$], D – net radiation [$R_n$], E – Air surface temperature [blue line] and surface relative humidity [RH – orange line]. In A, B and C black lines and white stars represent air temperature and $PBLH_{MWR}$, respectively.

Figure 9,12: Which instrument is this figure from?

We thank the Reviewer 1 for this question. As indicated in the title of these figures, the RCS profile is obtained from MULHACEN (the Raman lidar system) data.

This is a time-height plot of RCS, not a profile.

We thank the Reviewer 1 for this comment. In order to clarify this point the label of figures has been changed as follow:

"Time-Height plot of RCS …"

Analyzing the turbulent Planetary Boundary Layer behavior by the synergic use of remote sensing systems: Doppler wind lidar, aerosol elastic lidar and microwave radiometer

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Abstract

The Planetary Boundary Layer (PBL) is the lowermost region of troposphere and endowed with turbulent characteristics, which can have mechanical and/or thermodynamic origins. Such behavior gives to this layer great importance, mainly in studies about pollutant dispersion and weather forecasting. However, the instruments usually applied in studies about turbulence in the PBL have limitations in spatial resolution (anemometer towers) or temporal resolution (instrumentation onboard aircraft). In this study we propose the synergetic use of remote sensing systems (microwave radiometer [MWR], Doppler lidar [DL] and elastic lidar [EL]) to analyze the turbulent PBL behavior. Furthermore, we show how some meteorological variables such as air temperature, aerosol number density, vertical wind speed, relative humidity and net radiation might influence the turbulent PBL dynamic.The statistical moments of the high frequency distributions of the vertical wind velocity, derived from DL and of the backscattered coefficient derived from EL, are corrected by two methodologies, namely first lag and -2/3 correction. The corrected profiles present small differences when compared against the uncorrected profiles, showing low influence of noise and the viability of the proposed methodology. Two case studies were analyzed in detail, one corresponding to a well-defined PBL and another one corresponding to a situation with presence of a Saharan dust lofted aerosol layer and clouds. In both cases the results provided by the different instruments are complementary, thus the synergistic use of the different systems allow us performing a detailed monitoring of the turbulent PBL behavior, as well as, a better understanding about how the analyzed variables can interfere in this process.

Keywords: Turbulence, Planetary Boundary Layer, Doppler lidar, elastic lidar, microwave radiometer, Earlinet.

1 Introduction

The Planetary Boundary Layer (PBL) is the atmospheric layer directly influenced by the Earth's surface that responds to its changes within time scales around an hour (Stull, 1988). Such layer is located at the lowermost region of troposphere, and is mainly characterized by turbulent and cyclic processes, which are responsible of its large variability along the day processes and a daily evolution cycle. In an ideal situation, instants after sunrise, ground surface temperature increase due to the positive net radiative flux (R_n). This process intensifies the convection, thus, the ascending warm air masses heat the air masses situated in the upper regions of troposphere, originating the Convective Boundary Layer (CBL) or Mixing Layer (ML), which has this name due to a mixing process generated by this turbulent ascending air parcels. Some instants before sunset the gradual reduction of incoming solar irradiance at the Earth's surface causes the decrease of the positive R_n and its change in sign. In this situation, there is a reduction of the convective processes and a weakening of the turbulence. In this process the CBL leads to the development of two layers, namely a stably stratified boundary layer called Stable Boundary Layer (SBL) close to the surface, and the Residual Layer (RL) that contains features from the previous day's ML and is just above the SBL.

Knowledge of the turbulent processes in the CBL is important in diverse studies, mainly for atmospheric modeling and pollutant dispersion, since turbulent mixing can be considered as the primary process by which aerosol particles and other scalars are transported vertically in atmosphere. Because turbulent processes are treated as nondeterministic, they are characterized and described by their statistical properties (high order statistical moments). When applied to atmospheric studies such analysis provide information about the field of turbulent fluctuation, as well as, a description of the mixing process in the PBL (Pal et al., 2010).

Anemometer towers have been widely applied in studies about turbulence (e.g., Kaimal and Gaynor, 1983; van Ulden and Wieringa, 1996), however the limited vertical range of these equipment restrict the analysis to regions close to surface. Aircraft have also been used in atmospheric turbulence studies (e.g., Lenschow et al., 1980; Williams and Hacker, 1992; Lenschow et al., 1994; Albrecht et al., 1995; Stull et al., 1997; Andrews et al., 2004; Vogelmann et al., 2012), nevertheless their short time window limits the analysis. In this scenario, systems with high spatial and temporal resolution and enough range are necessary in order to provide more detailed results along the day throughout the whole thickness of the PBL.

In the last decades, lidar systems have been increasingly applied in this kind of study due to its their large vertical range, high data acquisition rate and capability to detect several observed quantities such as vertical wind velocity [Doppler lidar] (e.g. Lenschow et al., 2000; Lothon et al., 2006; O'Connor et al., 2010), water vapor [Raman lidar and DIAL] (e.g. Wulfmeyer, 1999; Kiemle et al., 2007; Wulfmeyer et al., 2010; Turner et al., 2014; Muppa et al., 2015), temperature [rotational Raman lidar] (e.g. Behrendt et al., 2015) and aerosol [elastic lidar] (e.g. Pal et al., 2010; McNicholas et al., 2015). This allows the observation of a wide range of atmospheric processes. For example, Pal et al. (2010) demonstrated how the statistical analyses obtained from high-order moments of elastic lidar can provide information about aerosol plume dynamics in the PBL region. In addition, when different lidar systems operate synergistically, as for example in Engelmann et al. (2008), who combined elastic and Doppler lidar data, it is possible to identify very complex variables such as vertical particle flux. However, this subject requires more exploration, mainly the synergy among lidar and others remote sensing systems, like microwave radiometer. Thus, the combination of information obtained from these instruments can provide a more detailed understanding about the turbulent PBL behavior. Such approach is even more attractive when considering facilities of networks, e. g. European Aerosol Research Lidar NETwork (EARLINET) (Pappalardo et al., 2014), Microwave Radiometer Network (MWRNET) (Rose et al., 2005; Caumont et al., 2016) and ACTRIS CLOUDNET (Illingworth et al., 2007).

Therefore, considering this scenario, in this study we use synergistically the data of three remote sensing systems (Elastic Lidar [EL], Doppler Lidar [DL] and Microwave Radiometer [MWR]) acquired during the SLOPE-I campaign, held at IISTA-CEAMA (Andalusian Institute for Earth System Research, Granada, Spain) from May to August 2016, in order to analyze the turbulent PBL behavior and to improve our comprehension about how each analyzed variable influence the PBL dynamics.

This paper is organized as follows. Description of the experimental site and the equipment setup are presented in Section 2. The methodologies applied are introduced in Section 3. Section 4 presents the results of the analyses using the different methodologies. Finally, conclusions are summarized in Section 5.

2 Experimental site and instrumentation

The SLOPE-I (Sierra nevada Lidar aerOsol Profiling Experiment) campaign was performed from May to September 2016 in South-Eastern Spain in the framework of the European **Research Infrastructure** for the observation of **Aerosol, Clouds, and Trace gases (**ACTRIS). The main objective of this campaign was to perform a closure study by comparing remote sensing system retrievals of atmospheric aerosol properties, using remote systems operating at the Andalusian Institute of Earth System Research (IISTA-CEAMA) and in-situ measurements operating at ~~distinct~~ different altitudes in the Northern slope of Sierra Nevada, around 20 km away from IISTA-CEAMA (Bedoya-Velásquez et al., 2018; Román et al., 2018). The IISTA-CEAMA station is part of EARLINET (Pappalardo et al, 2014) since 2005 and at present is an ACTRIS station (http://actris2.nilu.no/). The research facilities are located at Granada, a medium size city in Southeastern Spain (Granada, 37.16°N, 3.61°W, 680 m a.s.l.), surrounded by mountains and with Mediterranean-continental climate conditions that are responsible ~~of~~ for cool winters and hot summers. Rain is scarce, especially from late spring to early autumn. Granada is affected by different kind of aerosol particles locally originated and medium-long range transported from Europe, Africa and North America (Lyamani et al., 2006; Guerrero-Rascado et al., 2008, 2009; Titos et al., 2012; Navas-Guzmán et al., 2013; Valenzuela et al., 2014, Ortiz-Amezcua et al, 2014, 2017).

MULHACEN is a biaxial ground-based Raman lidar system operated at IISTA-CEAMA in the frame of EARLINET research network. This system operates with a pulsed Nd:YAG laser, frequency doubled and tripled by Potassium Dideuterium Phosphate crystals, emitting at wavelengths of 355, 532 and 1064 nm with output energies per pulse of 60, 65 and 110 mJ, respectively. MULHACEN operates with three elastic channels: 355, 532 (parallel and perpendicular polarization) and 1064 nm and three Raman-shifted channels: 387 (from N_2), 408 (from H_2O) and 607 nm (from N_2). MULHACEN's overlap is complete at 90% between 520 and 820 m a.g.l. for all the wavelengths, reaching full overlap around 1220 m a.g.l. (Navas-Guzmán et al ., 2011; Guerrero-Rascado et al. 2010). Calibration of the depolarization capabilities is done following Bravo-Aranda et al. (2013). This system was operated with a temporal and spatial resolution of 2 s and 7.5 m, respectively. More details can be found at Guerrero-Rascado et al. (2008, 2009).

The Doppler lidar (Halo Photonics, model Stream Line XR) is also operated at IISTA-CEAMA. This system works in continuous and automatic mode from May 2016. It operates at 1.5 µm with pulse energy and repetition rate of 100 µJ and 15 KHz, respectively. This system record the backscattered signal with 300 gates, being the range gate length 30 m, with the first gate at 60 m. The telescope focus is set to approximately 800 m. For this work the data were collected in stare mode (laser beam is pointed at vertical with respect to the ground surface) with a time resolution of 2 s.

Furthermore, we operated the ground-based passive microwave radiometer (RPG-HATPRO G2, Radiometer Physics GmbH), which is member of the MWRnet [http://cetemps.aquila.infn.it/mwrnet/]. This system operates in automatic and continuous mode at IISTA-CEAMA since November 2011. The microwave radiometer (MWR) measures the sky brightness temperature with a radiometric resolution between 0.3 and 0.4 K root mean square error at 1 s integration time, using direct detection receivers within two bands: K-band (water vapor – frequencies: 22.24 GHz, 23.04 GHz, 23.84 GHz, 25.44 GHz, 26.24 GHz, 27.84 GHz, 31.4 GHz) and V-band (oxygen – frequencies: 51.26 GHz, 52.28 GHz, 53.86 GHz, 54.94 GHz, 56.66 GHz, 57.3 GHz, 58.0 GHz). From these bands is possible to obtain profiles of water vapor and temperature, respectively, by inversion algorithms described in Rose et al. (2005). The range resolution of these profiles vary between 10 and 200 m in the first 2 km and between 200 and 1000 m in the layer between 2 and 10 km (Navas-Guzmán et al., 2014).

The meteorological sensor (HMP60, Vaisala) is used to register the air surface temperature and surface relative humidity, with a temporal resolution of 1 minute. Relative humidity is monitored with an accuracy of ± 3%, and air surface temperature is acquired with an accuracy and precision of 0.6° C and 0.01° C, respectively.

A CM-11 pyranometer manufactured by Kipp & Zonen (Delft, The Netherlands) is also installed in the ground-based station. This equipment measures the shortwave (SW) solar global horizontal irradiance data (305–2800 nm). The CM-11 pyranometer complies with the specifications for the first-class WMO (World Meteorological Organization) classification of this instrument (resolution better than ±5 Wm^{-2}), and the calibration factor stability has been periodically checked against a reference CM-11 pyranometer (Antón et. al, 2012).

3 Methodology

3.1 MWR data analysis

The MWR data are analyzed combining two algorithms, Parcel Method $[PM]$ (Holzworth, 1964) and Temperature Gradient Method $[TGM]$ (Coen, 2014), in order to estimate the PBL Height ($PBLH_{MWR}$) in convective and stable situations, respectively. The different situations are discriminated by comparing the surface potential temperature ($\theta(z_0)$) with the corresponding vertical profile of $\theta(z)$ up to 5 km. Those cases where all the points in the vertical profile have values larger than $\theta(z_0)$ are labeled as stable, and TGM is applied. Otherwise the situation is labeled as unstable and the PM is applied. The vertical profile of $\theta(z)$ is obtained from the vertical profile of T(z) using the following equation (Stull, 2011):

$$\theta(z) = T(z) + 0.0098 * z \quad (1)$$

where $T(z)$ is the temperature profile provided by MWR, z is the height above the sea level, and 0.0098 K/m is the dry adiabatic temperature gradient. A meteorological station co-located with the MWR is used to detect the surface temperature [$T(z_0)$]. In order to reduce the noise, $\theta(z)$ profiles were averaged providing a $PBLH_{MWR}$ value at 30 minutes intervals. This methodology of $PBLH$ detection was selected as the reference due to the results obtained during a performed campaign of comparison between MWR and radiosonde data, where twenty-three radiosondes were launched. High correlations were found between $PBLH$ retrievals provided by both instruments in stable and unstable cases. Further details are given by Moreira et al. (2018a).

3.2 Lidar turbulence analysis

Both lidar systems, DL and EL, gathered data with a temporal resolution of 2 seconds. Then, the data are averaged in 1-hour packages, from which the mean value is extracted [$\bar{q}(z)$]. Such mean value is subtracted from each $q(z,t)$ profile in order to estimate the vertical profile of the fluctuation for the measured variable [$q^{'}(z,t)$] (i.e. vertical velocity for the DL):

$$q^{'}(z,t) = q(z,t) - \bar{q}(z) \quad (2)$$

Then, from $q^{'}(z,t)$ is possible to obtain the high-order moments (variance ($\boldsymbol{\sigma}^2$), skewness ($\boldsymbol{S}$) and kurtosis ($\boldsymbol{K}$)), as well as, the integral time scale ($\boldsymbol{\tau}$ - which is the time over which the turbulent process are highly correlated to itself) as shown in Table 1. These variables can also be obtained from the following autocovariance function, M_{ij}:

$$M_{ij} = \int_0^{t_f} [q^{'}(z,t)]^i [q^{'}(z,t + t_f)]^j dt \quad (3)$$

where t_f is the final time, i and j indicate the order of autocovariance function.

However, it is necessary to considerer that the acquired real data contain instrumental noise, $\varepsilon(z)$. Therefore, the equation 3 can be rewritten as:

$$M_{ij} = \int_0^{\tau} [q(z,t) + \varepsilon(z,t)]^i [q(z,t + \tau) + \varepsilon(z,t + \tau)]^j dt \quad (4)$$

The autocovariance function of a time series with zero lag results in the sum of the variances of the atmospheric variable and its $\varepsilon(z)$. Nevertheless, atmospheric fluctuations are correlated in time, but the $\varepsilon(z)$ is random and uncorrelated with the atmospheric signal. Consequently, the noise is only associated with lag 0 (Fig. 1). Based on this concept Lenschow et al. (2000) suggested to obtain the corrected autocovariance function, $M_{11}(\rightarrow 0)$, from two methods, namely first lag correction or -2/3 law correction. In the first method, $M_{11}(\rightarrow 0)$ is obtained directly by the subtraction of lag 0, $\Delta M_{11}(0)$, from the autocovariance function, $M_{11}(0)$. In the second method $M_{11}(\rightarrow 0)$ is generated by the extrapolation of $M_{11}(0)$ at firsts nonzero lags back to lag zero (-2/3 law correction). The extrapolation can be performed using the inertial subrange hypothesis, which is described by the following equation (Monin and Yaglom, 1979):

$$M_{11}(\rightarrow 0) = \overline{q'^2(z,t)} + Ct^{2/3} \quad (5)$$

where C represents a parameter of turbulent eddy dissipation rate. The high-order moments and $\boldsymbol{\tau}$ corrections and errors are shown in Table 1 (columns 2 and 3, respectively).

The same procedure of analysis is applied in studies with DL and EL, being the main difference the tracer used by each system, which are the fluctuation of vertical wind speed (w') for DL and aerosol number density (N') for EL. DL provides $w(z,t)$ directly, and therefore the procedure described in Figure 2 can be directly applied. Thus, the two corrections described above are applied separately and finally $\boldsymbol{\tau}$ and high-order moments with and without corrections can be estimated.

On the other hand, the EL does not provide $N(z,t)$ directly. Under some restrictions, it is possible to ignore the particle hygroscopic growth and to assume that the vertical distribution of aerosol type does not changes with time, and to adopt the following relation (Pal et al., 2010):

$$\beta_{par}(z,t) \approx N(z,t)Y(z) \ \Rightarrow \beta'_{par}(z,t) = N'(z,t) \quad (6)$$

where β_{par} and β'_{par} represent the particle backscatter coefficient and its fluctuation, respectively, and Y does not depends on time.

Considering the lidar equation:

$$P_\lambda(z) = P_0 \frac{ct_d}{2} AO(z) \frac{\beta_\lambda(z)}{z^2} e^{-2\int_0^z \alpha_\lambda(z')dz'} \quad (7)$$

where $P_\lambda(z)$ is the signal returned from distance z at time t, z is the distance [m] from the lidar of the volume investigated in the atmosphere, P_0 is the power of the emitted laser pulse, c is the light speed [m/s], t_d is the duration of laser pulse [ns], A is the area [m²] of telescope cross section, $O(z)$ is the overlap function, $\alpha_\lambda(z)$ is the total extinction coefficient (due to atmospheric particles and molecules) [(km)$^{-1}$] at distance z, $\beta_\lambda(z)$ is the total backscatter coefficient (due to atmospheric particles and molecules) [(km·sr)$^{-1}$] at distance z and the subscript λ represents the wavelength. The two path transmittance term related to $\alpha(z)$ is considered as nearly negligible at 1064 nm (Pal et al., 2010). Thus, it is possible to affirm that:

$$RCS_{1064}(z) = P(z)_{1064}.z^2 \cong G.\beta_{1064}(z) \quad (8)$$

and consequently:

$$RCS'_{1064}(z,t) \cong \beta'_{1064}(z,t) = \beta'_{par}(z,t) = N'(z,t) \quad (9)$$

where RCS_{1064} and RCS'_{1064} are the range corrected signal and its fluctuation, respectively, G is a constant and the subscripts represent the wavelength.

In this way, Pal et al. (2010) have shown the feasibility of using EL operating at 1064 nm for describing the atmospheric turbulence. In a recent paper Moreira et al. (2018b), have shown that the use of the EL at 532 nm, in spite of the larger attenuation expected at this wavelength due to both aerosol and molecules, provides a description of the turbulence equivalent to that provided by EL operating at 1064 nm. This result is interesting having in mind the more extended use of lidar systems based on laser emission at 532 nm in different coordinated networks. Thus, in EARLINET and LALINET (Latin American LIdar NETwork) around 76% and 45% of the systems include the wavelength of 1064 nm, while 95% of the EARLINET systems and 73% of the LALINET systems operate systems that include the wavelength 532 nm (Guerrero-Rascado et al., 2016). Furthermore, the performance of the lidar systems at 532 nm presents better signal to noise ratio than that encountered at 1064nm. Thus, in this study we use the RCS_{532} for analyzing turbulence using EL, following the procedure described in Figure 3, which is basically the same methodology described earlier for DL.

These three methodologies, together with data of net surface radiation (obtained from pyranometer data) and air temperature (provided by MWR), are used synergistically in order to complement one each other and consequently generate a detailed picture of how each variable influences the turbulent PBL behavior, as it will be demonstrated in subsection 4.2.

4 Results

4.1 Error Analysis

The influence of random error in noisy observations rapidly grows for higher-order moments (i.e., the influence of random noise is much larger for the fourth-order moment than for the third-order moment). Therefore, the first step, in order to ascertain the applied methodology and our data quality, we performed the error treatment of DL data as described in Figure 2.

Figure 4 illustrates the autocovariance function, generates from w', at three different heights. As mentioned before, the lag 0 is contaminated by noise ε, and thus the impact of the noise ε increases together with height, mainly above $PBLH_{MWR}$ (1100 m a.g.l. in our example).

Figure 5-A illustrates the comparison between integral time scale ($\boldsymbol{\tau_{w'}}$) without correction and the two corrections cited in section 3.2. Except for the first height, under the $PBLH_{MWR}$ the profiles practically do not have significant difference, as well as small errors bars. Above $PBLH_{MWR}$ the first lag correction presents some differences in relation the other profiles at around 1350 m.

Figures 5-B and 5-C show the comparison of variance ($\boldsymbol{\sigma}_{w'}^2$) and skewness ($\boldsymbol{S}_{w'}$), respectively, with and without corrections. The profiles corrected by -2/3 law do not present significant differences in comparison to uncorrected profiles. On the other hand, the profiles corrected by the first lag correction have significant differences under the $PBLH_{MWR}$, mainly the $\boldsymbol{\sigma}_{w'}^2$ ($\boldsymbol{S}_{w'}$ only in the first 50 m**)**, and some slight differences are evident above $PBLH_{MWR}$.

For EL we use the same procedure for the correction and error analysis that we apply to the DL data. Figure 6 shows the autocovariance function, obtained from RCS', at three distinct heights. As expected, the increase of height produces the increase of ε, principally above the $PBLH_{MWR}$.

Figures 7-A, 7-B, 7-C and 7-D show the vertical profiles of $\boldsymbol{\tau}_{RCS'}$, $\boldsymbol{\sigma}_{RCS'}^2$, $\boldsymbol{S}_{RCS'}$ and kurtosis ($\boldsymbol{K}_{RCS'}$), respectively, with and without the corrections described in section 3.2. In general, the corrections do not affect the profiles in a significant way, especially in the region below the $PBLH_{MWR}$. Above the $PBLH_{MWR}$ some small differences are noticed, mainly in the first lag correction. The error bars associated to each profile also have low values in all cases. When comparing corrected and uncorrected profiles, the largest differences are observed for the profiles at higher order moments, because of error propagation. $\boldsymbol{K}_{RCS'}$ profile is the more affected by corrections, so the kurtosis profile after the first lag correction shows the largest difference with uncorrected profile.

Since the first lag and 2/3 corrections do not have a significant impact within the PBL region, we adopted the first lag correction in order to be more careful during the comparison.

4.2 Case studies

In this section we present two study cases, in order to show how the synergy of methodologies described in section 3 can provide a detailed description about the turbulent PBL behavior. The first case represents a typical day with a clear sky situation. The second case corresponds to a more complex situation, where there is presence of clouds and Saharan mineral dust layers.

4.2.1 Case study I: clear sky situation

In this case study we use measurements gathered with DL, MWR and pyranometer during 24 hours. The EL was operated under operator-supervised mode between 08:20 to 18:00 UTC.

Figure 8 (A) shows the integral time scale obtained from DL data ($\boldsymbol{\tau}_{w'}$). The gray areas represents the region where $\boldsymbol{\tau}_{w'}$ is lower than the acquisition time of DL and, therefore, for this region it is not possible to analyze turbulent processes. However, the gray area is located almost entirely above the $PBLH_{MWR}$ (white stars). Thus, the DL acquisition time allows us to observe the turbulence throughout the whole PBL. The gray areas, as well as, the black lines (air temperature), have the same meaning in Figures 8-B and 8-C.

$\boldsymbol{\sigma}^2_{\mathbf{w}'}$ has low values during the entire period of SBL (Figure 8-B). Nevertheless, as air temperature begins to increase (around 07:00 UTC), $\boldsymbol{\sigma}^2_{\mathbf{w}'}$ increases together, as well as, $PBLH_{MWR}$. $\boldsymbol{\sigma}^2_{\mathbf{w}'}$ reaches its maximum values in the middle of the day, when we also observe the maximum values of air temperature and $PBLH_{MWR}$. This process is in agreement with the behavior of skewness of w' ($\mathbf{S}_{\mathbf{w}'}$) shown in Figure 8-C. $\mathbf{S}_{\mathbf{w}'}$ is directly associated with the direction of turbulent movements. Thus, positive values correspond with a surface-heating-driven boundary layer, while negative ones are associated to cloud-top long-wave radiative cooling. If $\mathbf{S}_{\mathbf{w}'}$ is positive, both $\boldsymbol{\sigma}^2_{\mathbf{w}'}$ and TKE (Turbulent Kinetic Energy) are being transported upwards and consequently, the red regions in Figure 13-C represent positive values of $\mathbf{S}_{\mathbf{w}'}$ and the blue regions refer to negative ones. During the stable period, there is predominance of low values of $\mathbf{S}_{\mathbf{w}'}$. Nevertheless, as air temperature increases (transition from stable to unstable period), $\mathbf{S}_{\mathbf{w}'}$ values begin to become positive and increase with the ascent of the $PBLH_{MWR}$ (CBL). Air temperature begins to decrease around 18:00 UTC, causing the reduction of $\mathbf{S}_{\mathbf{w}'}$. In this moment the transition from unstable to stable period occurs and, therefore, the reduction in $PBLH_{MWR}$ is due to the $SBLH$ detection.

Figure 8-D shows the values of net surface radiation (R_n) that are estimated from solar global irradiance values using the seasonal model described in Alados et al. (2003). The negative values of R_n are concentrated in the stable region. R_n begins to increase around 06:00 UTC and reaches its maximum in the middle of the day. Comparing figures 8-C and 8-D, we can observe similarity among the behavior of $\mathbf{S}_{\mathbf{w}'}$, R_n and surface air temperature, because these variables increase and decrease together, as expected.

The increase of R_n causes the rise of surface air temperature, which contributes to the positive latent heat flux from the surface ($\mathbf{S}_{\mathbf{w}'}$) and, consequently, the growth of the $PBLH_{MWR}$ (CBL). $\mathrm{R_n}$ begins to decrease certain time before the other variables, but the intense reduction of air temperature and decrease of $\mathbf{S}_{\mathbf{w}'}$ and $SBLH$ detection occurs when R_n becomes negative again, although there can still be a positive sensible heat flux, what is characteristic of early evening in urban regions due to the release of the ground heat flux at that time.

Figure 8-E presents the values of surface air temperature and surface relative humidity (RH). Air surface temperature is directly related with R_n and $\mathbf{S}_{\mathbf{w}'}$ values, as aforementioned and expected. On the other hand, RH is inversely correlated with temperature and, thus, with the rest of variables, due to the relative constancy of the water vapor mixing ratio characteristic of our site during the study

Figure 9 shows the RCS_{532} profile obtained from 08:00 to 18:00 UTC and the well-defined $PBLH_{MWR}$ (pink stars). At the beginning of the measurement period (08:20 to 10:00 UTC) it is possible to observe the presence of a thin residual layer (around 2000 m a.s.l.), and later from 13:00 to 18:00 UTC it is evident a lofted aerosol layer. The period between 13:00 and 14:00 UTC has been selected to be analyzed. Figure 10-A presents the profiles of molecular ($\beta_{Molecular}$) and aerosol ($\beta_{Aerosol}$) backscatter coefficients at 532 nm. Although β_{532} is composed by $\beta_{Molecular}$ and $\beta_{Aerosol}$, it is possible to observe the predominance of $\beta_{Aerosol}$ in the region below of the $PBLH_{MWR}$, as demonstrated in figure 10-B by the β_{Ratio} profile. Similar results were demonstrated by Moreira et al. (2018b), therefore reinforcing the viability of the use of this wavelength in studies about turbulence. Figure 11 presents the statistical moments generated from RCS', which were obtained from 13:00 and 14:00 UTC. The maximum for the variance of RCS can be used as indicator of $PBLH$ ($PBLH_{Elastic}$) (Moreira et al., 2015). Thus, the red line in all graphics represent the $PBLH_{Elastic}$ (2200 m a.s.l.) and the blue one the average value of $PBLH_{MWR}$ (2250 m a.s.l.), both obtained between 13 and 14 UTC.

Due to well-defined PBL, $PBLH_{Elastic}$ and $PBLH_{MWR}$ do not have significant differences (50 m). $\boldsymbol{\sigma}^2_{RCS'}$ has small values below the $PBLH$. Above $PBLH_{Elastic}$ the values of $\boldsymbol{\sigma}^2_{RCS'}$ decrease slowly due to location of the lofted aerosol around 2500 m. However, above this aerosol layer the value of $\boldsymbol{\sigma}^2_{RCS'}$ is reduced to zero, indicating the extreme decreasing in aerosol concentration in the free troposphere. The integral time scale obtained from RCS' ($\boldsymbol{\tau_{RCS'}}$) has values higher than EL time acquisition throughout the CBL, evidencing the feasibility for studying turbulence using this elastic lidar configuration. The skewness values obtained from RCS' ($\boldsymbol{S_{RCS'}}$) give us information about aerosol motion. The positive values of $\boldsymbol{S_{RCS'}}$ observed in the lowest part of profile and above the $PBLH_{Elastic}$ represents the updrafts aerosol layers. The negative values of $\boldsymbol{S_{RCS'}}$ indicates the region with low aerosol concentration due to clean air coming from free troposphere (FT). This movement of ascension of aerosol layers and descent of clean air with zero value of $\boldsymbol{S_{RCS'}}$ is characteristic of growing PBL and was also detected by Pal et al. (2010) and McNicholas et al. (2014). The kurtosis of RCS' ($\boldsymbol{K_{RCS'}}$) determines the level of mixing at different heights. There are values of $\boldsymbol{K_{RCS'}}$ larger than 3 in the lowest part of profile and around 2500 m, showing a peaked distribution in this region. On other hand, values of $\boldsymbol{K_{RCS'}}$ lower than 3 are observed close to the $PBLH_{Elastic}$, therefore this region has a well-mixed CBL regime. Pal et al. (2010) and McNicholas et al. (2014) also detected this feature in the region nearby the $PBLH$.

The results provided by DL, pyranometer and MWR data agree with the results observed in Figure 10. In the same way, the analysis of high order moments of RCS' fully agree with the information in Figure 8. Thus, the large values of $\boldsymbol{S_{RCS'}}$ and $\boldsymbol{K_{RCS'}}$ detected around 2500 m a.s.l, where we can see a lofted aerosol layer, suggest the ascent of an aerosol layer and presence of a peaked distribution, respectively.

4.2.2 Case study: dusty and cloudy scenario

In this case study measurements with DL, MWR and pyranometer expand during 24 hours, while EL data are collected from 09:00 to 16:00 UTC.

Figure 12-A shows $\boldsymbol{\tau_{w'}}$, where the black lines and gray area has the same meaning mentioned earlier. Outside the period 13:00 to 17:00 UTC, the grey area is situated completely above the $PBLH_{MWR}$ (white stars), thus DL time acquisition is enough to perform studies about turbulence in this case.

$\boldsymbol{\sigma}^2_{w'}$ has values close to zero during all the stable period (Figure 12-B). However, when air temperature and $PBLH_{MWR}$ begins to increase (around 06:00 UTC), $\boldsymbol{\sigma}^2_{w'}$ also increases and reaches its maximum in the middle of the day. In the late afternoon, as air temperature and $PBLH_{MWR}$ decrease, the values of $\boldsymbol{\sigma}_{w'}^2$ decrease gradually, until reach the minimum value associated to the SBL. Figure 12-C shows the profiles of $\boldsymbol{S}_{w'}$. In the same way of the previous case study, the behavior of $\boldsymbol{S}_{w'}$ is directly related to the air temperature pattern (increasing and decreasing together) and causing the growth and reduction of $PBLH_{MWR}$. The main features of this case are: the low values of $\boldsymbol{S}_{w'}$, the **s**low increase and ascension of positive $\boldsymbol{S}_{w'}$ values and the predominance of negative $\boldsymbol{S}_{w'}$ values from 12:00 to 13:00 UTC. The first two features are likely due to the presence of the intense Saharan dust layer (Figure 13), which reduces the transmission of solar irradiance, and consequently the absorption of solar irradiance at the surface, generating weak convective process. From Figure 13 we can observe the presence of clouds from 12:00 to 14:00 UTC. This justifies the intense negative values of $\boldsymbol{S}_{w'}$ observed in this period, because, as mentioned before, $\boldsymbol{S}_{w'}$ is directly associated with direction of turbulent movements that during this period is associated to cloud-top long-wave radiative cooling, due to the presence of clouds (Ansmann et al., 2010).

The influence of Saharan dust layer can also be evidenced on the R_n pattern (Figure 12-D), which maintains negative values until 12:00 UTC and reaches a low maximum value (around 200 W/m²). Air surface temperature and RH (Figure 12-E) present the same correlation and anti-correlation (respectively) observed in the earlier case study, where the maximum of air surface temperature and the minimum of RH are detected in coincidence with the maximum daily value of $PBLH_{MWR}$.

As mentioned before, Figure 13 shows the RCS profile obtained from 09:00 to 16:00 UTC in a complex situation, with presence of decoupled dust layer (around 3800 m a.s.l.) from 09:00 and 12:00 and clouds (around 3500 m a.s.l.) from 11:00 to 16:00 UTC. The pink stars represent $PBLH_{MWR}$. Figure 14-A presents the $\beta_{Molecular}$ and $\beta_{Aerosol}$ profiles, similarly to Figure 10-A. It is evident the predominance of $\beta_{Aerosol}$ in the region below $PBLH_{MWR}$, as demonstrated by β_{Ratio} profile in figure 14-B. However due to presence of dust layer this dominance of $\beta_{Aerosol}$ is extended to approximately 4500 m a.s.l. Therefore the methodology proposed by Moreira et al. (2018b), based on considerations of Pal et al. (2010), can be applied.

Figure 15 illustrates the statistical moments of RCS' obtained from 11:00 to 12:00 UTC. The $\boldsymbol{\sigma}_{RCS'}^2$ profile presents several peaks due to the presence of distinct aerosol sublayers. The first peak is coincident with the value of $PBLH_{MWR}$. The value of $PBLH_{elastic}$, is coincident with the base of the dust layer. This difficulty to detect the $PBLH$ in presence of several aerosol layers is inherent to the variance method (Kovalev and Eichinger, 2004). The values of $\boldsymbol{\tau}_{RCS'}$ are higher than EL acquisition time all along the PBL, evidencing the feasibility of EL time acquisition for studying the turbulence of PBL in this case. The $\boldsymbol{S}_{RCS'}$ profile has several positive values, due to the large number of aerosol sublayers that are present. The characteristic inflection point of $\boldsymbol{S}_{RCS'}$ is observed in coincidence with the $PBLH_{MWR}$, that confirming the agreement between this point and the $PBLH$. $\boldsymbol{K}_{RCS'}$ has predominantly values lower than 3 below 2500 m, thus shown how this region is well mixed as can see in Figure 13. Values of $\boldsymbol{K}_{RCS'}$ larger than 3 are observed in the highest part of profile, where the dust layer is located.

Figure 16 shows the RCS' high-order moments obtained from 12:00 and 13:00 in presence of cloud cover. The method based on maximum of $\boldsymbol{\sigma}^2_{RCS'}$ locates the $PBLH_{Elastic}$ at the cloud base, due to the high variance of RCS' generated by the clouds. $\boldsymbol{\tau}_{\boldsymbol{RCS'}}$ presents values larger than EL time acquisition, therefore this configuration enable us to study turbulence by EL analyses. $\boldsymbol{S}_{\boldsymbol{RCS'}}$ has few peaks, due to the mixing between CBL and dust layer, generating a more homogenous layer. The highest values of $\boldsymbol{S}_{\boldsymbol{RCS'}}$ are observed in regions where there are clouds, and the negative ones (between 3500 and 4000 m) occur due to presence of air from FT between the two aerosol layers (Figure 13). The inflection point of $\boldsymbol{S}_{\boldsymbol{RCS'}}$ profile is observed in $PBLH_{MWR}$ region. $\boldsymbol{K}_{\boldsymbol{RCS'}}$ profile has low values in most of the PBL, demonstrating the high level of mixing during this period, where dust layer and PBL are combined. The higher values of $\boldsymbol{K}_{\boldsymbol{RCS'}}$ are observed in the region of clouds.

5 Conclusions

In this paper we analyze the turbulent PBL behavior and how each detected variable can influence it. Such observations were made from the synergy of three different types of remote sensing systems (DL, EL and MWR) and surface sensors during SLOPE-I campaign. We applied two kind of corrections to the lidar data: first lag and -2/3 corrections. The corrected DL statistical moments showed little variation with respect to the uncorrected profiles, denoting a rather low influence of the noise. The statistical moments obtained from EL also showed a small variation after correction when compared with the uncorrected profiles, except for $\mathrm{K}_{\mathrm{RCS'}}$, that is more affected by noise. The small changes in the profiles after the corrections, specially inside the PBL, evidence the feasibility of the applied methodology for monitoring the turbulence in the PBL. Nevertheless, all profiles are corrected by first lag correction, which is more restrictive during the comparison, in order to be cautious.

The case studies present two kind of situations: well-defined PBL and a more complex situation with the presence of Saharan dust layer and some clouds. $\sigma^2_{w'}$ and $S_{w'}$ showed a good agreement with the behavior of the air temperature, R_n and $PBLH_{MWR}$ in both situations, highlighting the feasibility in different atmospheric conditions.

The synergic use of remote sensing systems shows how the results provided by the different instruments can complement one each other. Thus, it is possible to observe the direct relationship among PBL growth, $S_{w'}$, $\sigma^2_{w'}$ $\sigma^2_{RCS'}$ and R_n values. In addition, $S_{RCS'}$ and $K_{RCS'}$ provide a good description about aerosol dynamic. The combination of these results gives us a detailed description about PBL dynamic and its structure.

Therefore, this study shows the feasibility of the described methodology based on remote sensing systems for studying the turbulence. The feasibility of using the analyses of high order moments of the RCS collected at 532nm at a temporal resolution of 2 s for the characterization of the atmospheric turbulence in the PBL offers the possibility for using this procedure in networks such as EARLINET or LALINET with a reasonable additional effort.

Acknowledgements

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Table 1 – Variables applied to statistical analysis (Lenschow et al., 2000)

	Without Correction	Correction	Error
Integral Time Scale (τ)	$\int_{0}^{\infty} q'(t)dt$	$\frac{1}{\overline{q'^2}}\int_{t\to 0}^{\infty} M_{11}(t)dt$	$\tau.\sqrt{\frac{4\Delta M_{11}}{M_{11}(\to 0)}}$
Variance ($\sigma_{q'}^2$)	$\frac{1}{T}\sum_{t=1}^{T}(q(t)-\overline{q})^2$	$M_{11}(\to 0)$	$q^2.\sqrt{\frac{4\Delta M_{11}}{M_{11}(\to 0)}}$
Skewness (S)	$\frac{\overline{q^3}}{\sigma_q^3}$	$\frac{M_{21}(\to 0)}{M_{11}^{3/2}(\to 0)}$	$\frac{\Delta M_{21}}{\Delta M_{11}^{3/2}}$
Kurtosis (K)	$\frac{\overline{q^4}}{\sigma_q^4}$	$\frac{3M_{22}(\to 0) - 2M_{31}(\to 0) - 3\Delta M_{11}^2}{M_{11}^2(\to 0)}$	$\frac{4\Delta M_{31} - 3\Delta M_{22} - \Delta M_{11}^2}{\Delta M_{11}^2}$

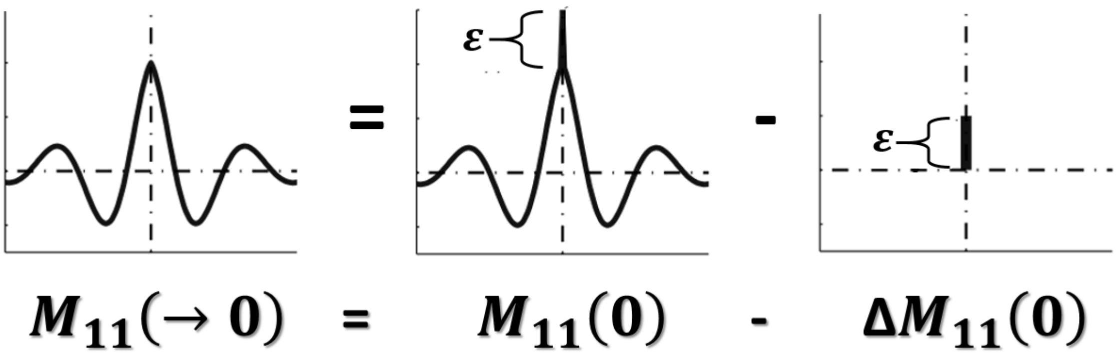

Figure 1 – Procedure to remove the errors of autocovariance functions. $M_{11}(\to 0)$ – corrected autocovariance function errors; $M_{11}(0)$ - autocovariance function without correction; $\Delta M_{11}(0)$ - error of autocovariance function

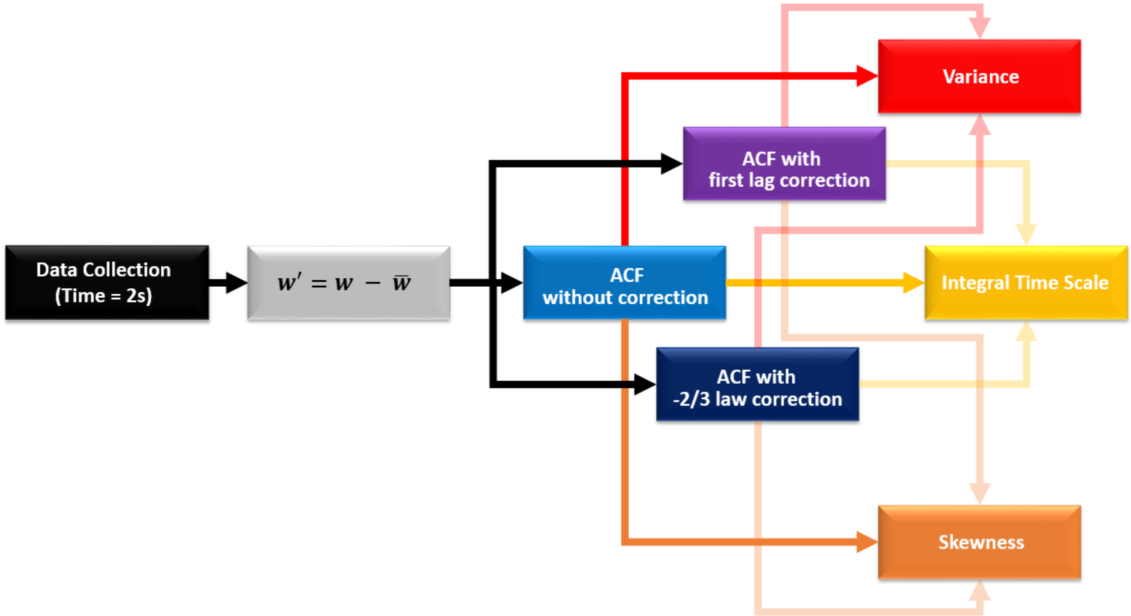

Figure 2 – Flowchart of data analysis methodology applied to the study of turbulence with Doppler lidar

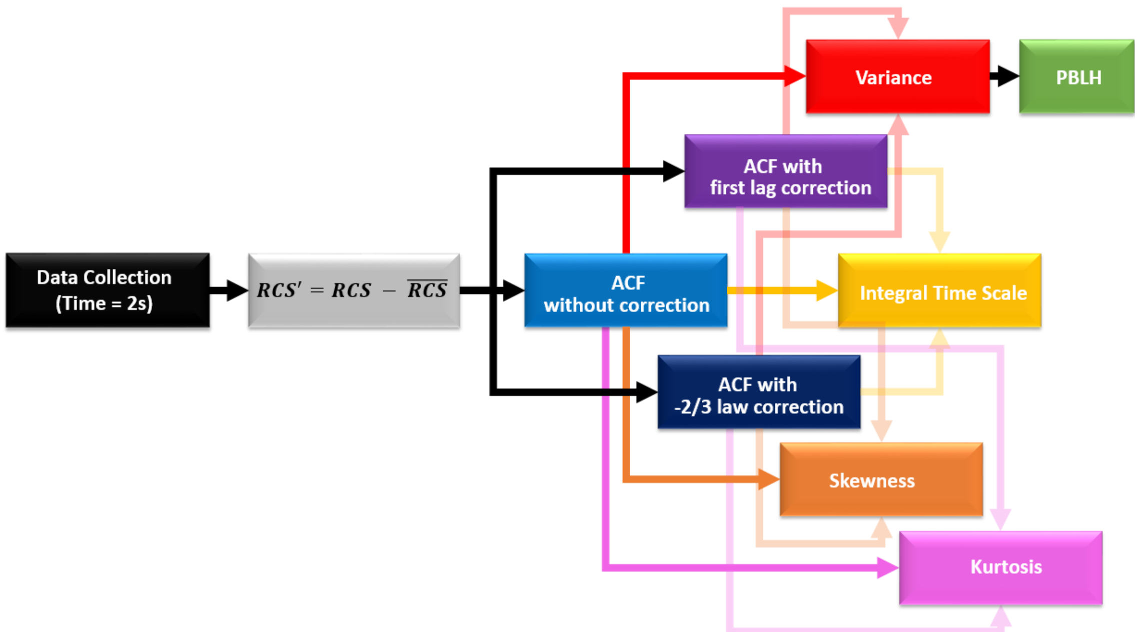

Figure 3 – Flowchart of data analysis methodology applied to the study of turbulence with elastic lidar

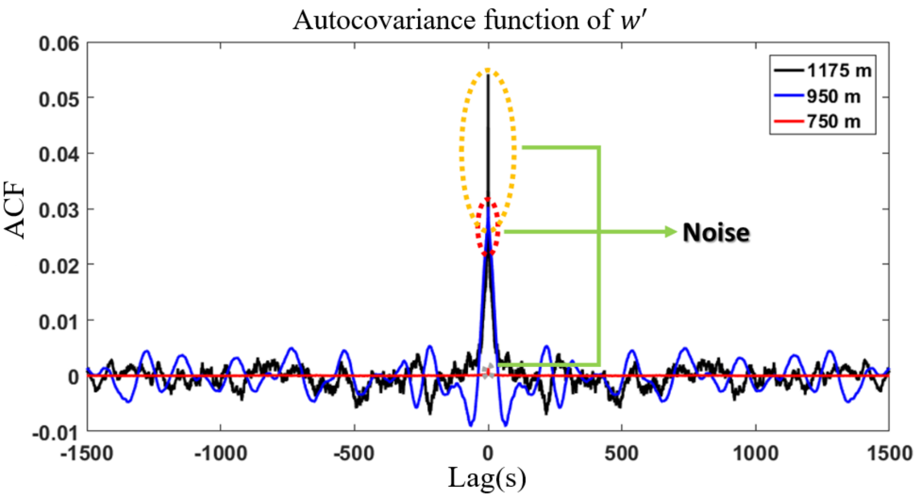

Figure 4 – Autocovariance function (ACF) of w' at three different heights

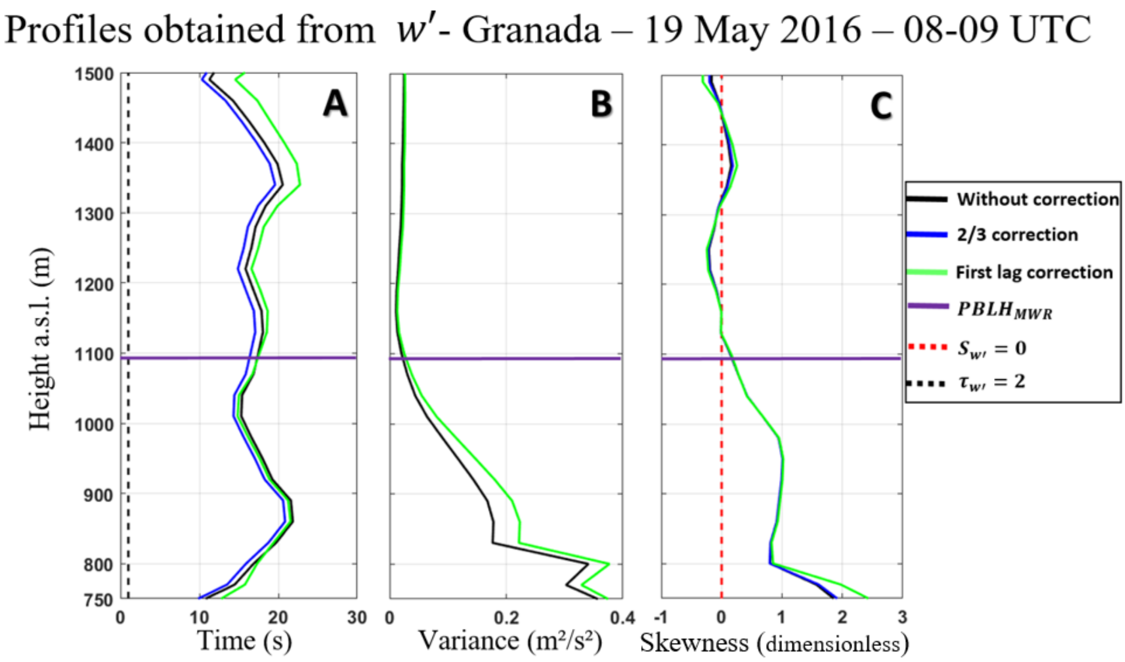

Figure 5 – A - Vertical profile of Integral time scale ($\tau_{w'}$). B - Vertical profile of variance ($\sigma^2_{w'}$). C - Vertical profile of Skewness. ($S_{w'}$)

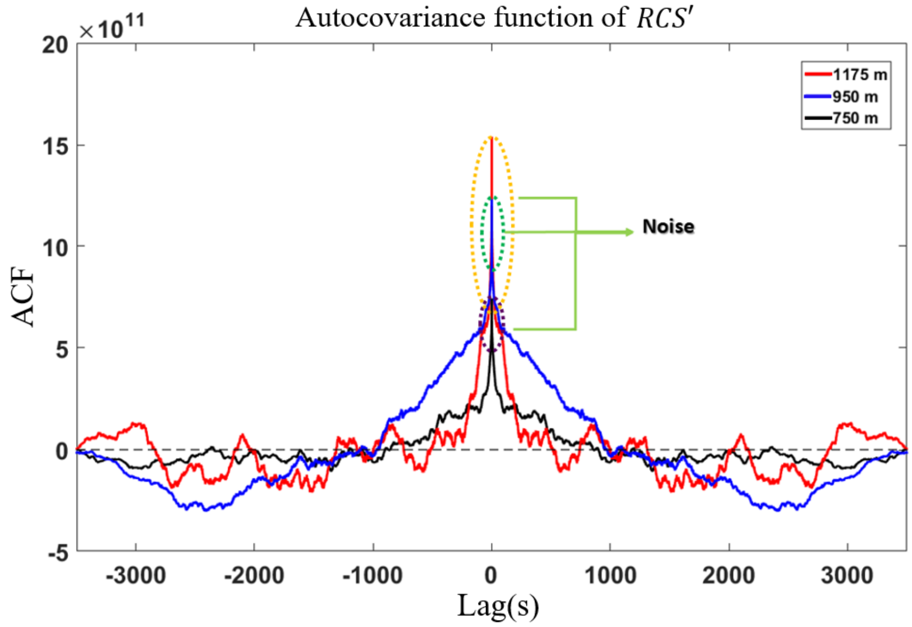

Figure 6 – Autocovariance of RCS' to three different heights

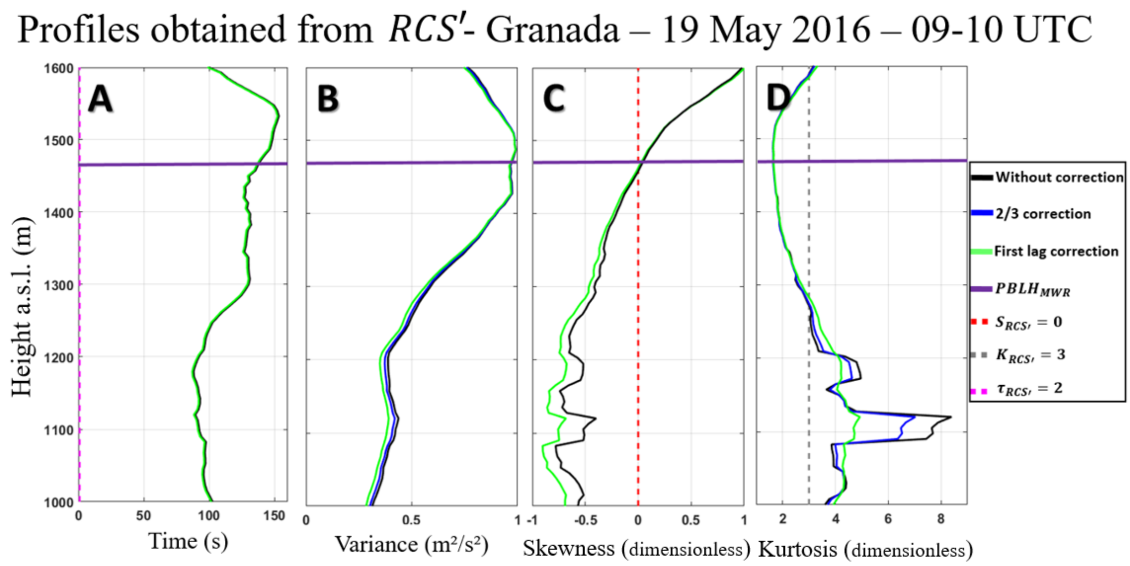

Figure 7 – A- Vertical profile of Integral time scale ($\boldsymbol{\tau_{RCS'}}$). B - Vertical profile of variance ($\boldsymbol{\sigma}^2_{RCS'}$). C - Vertical profile of Skewness ($\boldsymbol{S_{RCS'}}$). D - Vertical profile of Kurtosis ($\boldsymbol{K_{RCS'}}$).

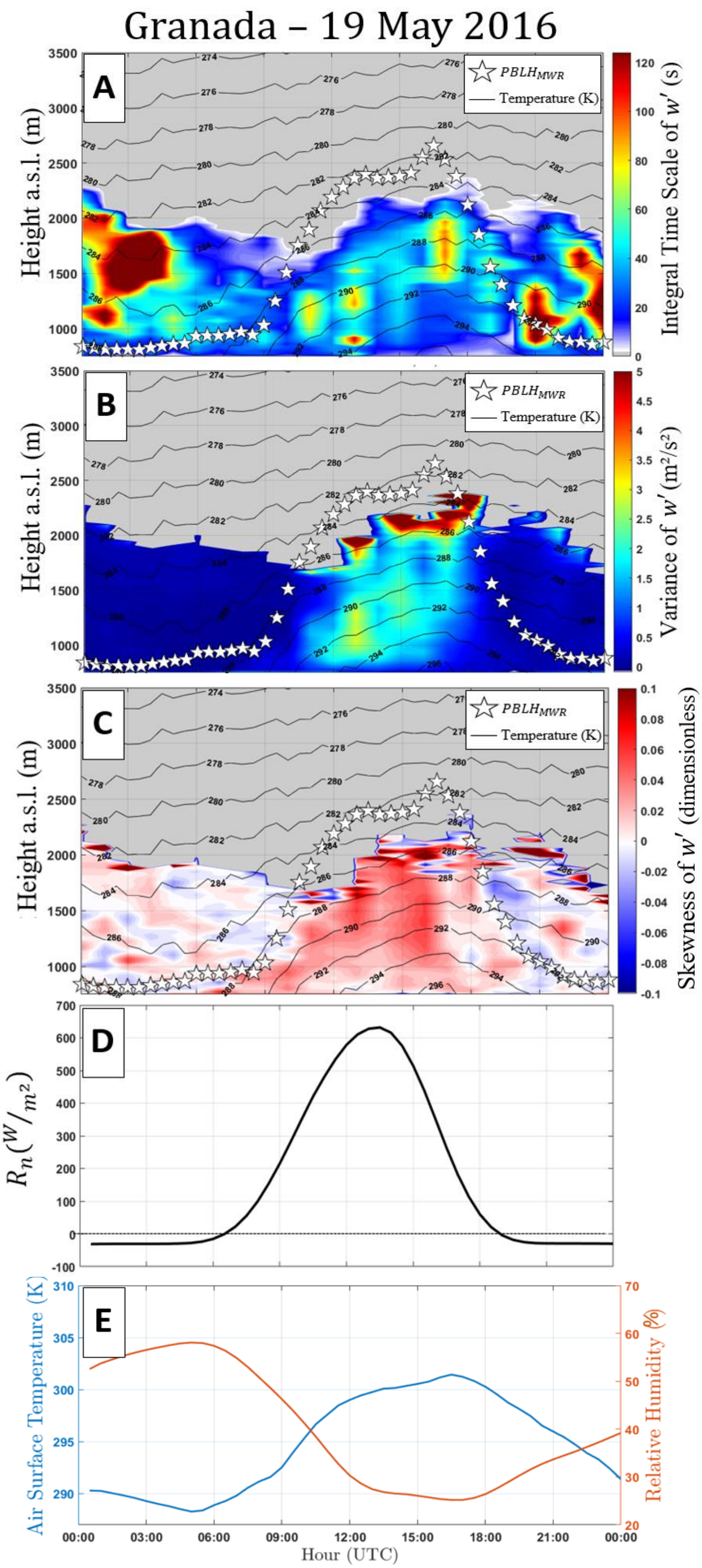

Figure 8 – A – integral time scale [$\boldsymbol{\tau_{w'}}$], B – variance [$\boldsymbol{\sigma}^2_{w'}$], C – skewness [$\boldsymbol{S_{w'}}$], D – net radiation [$R_n$], E – Air surface temperature [blue line] and surface relative humidity [RH – orange line]. In A, B and C black lines and white stars represent air temperature and $PBLH_{MWR}$, respectively.

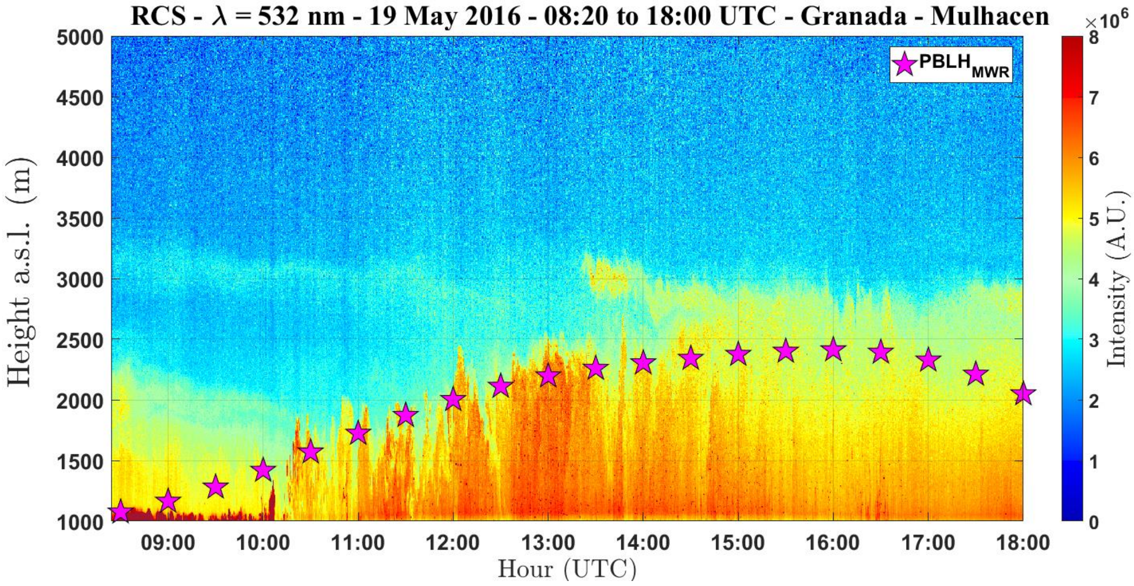

Figure 9 – Time-Height plot of RCS - 19 May 2016. Pink stars represent $PBLH_{MWR}$

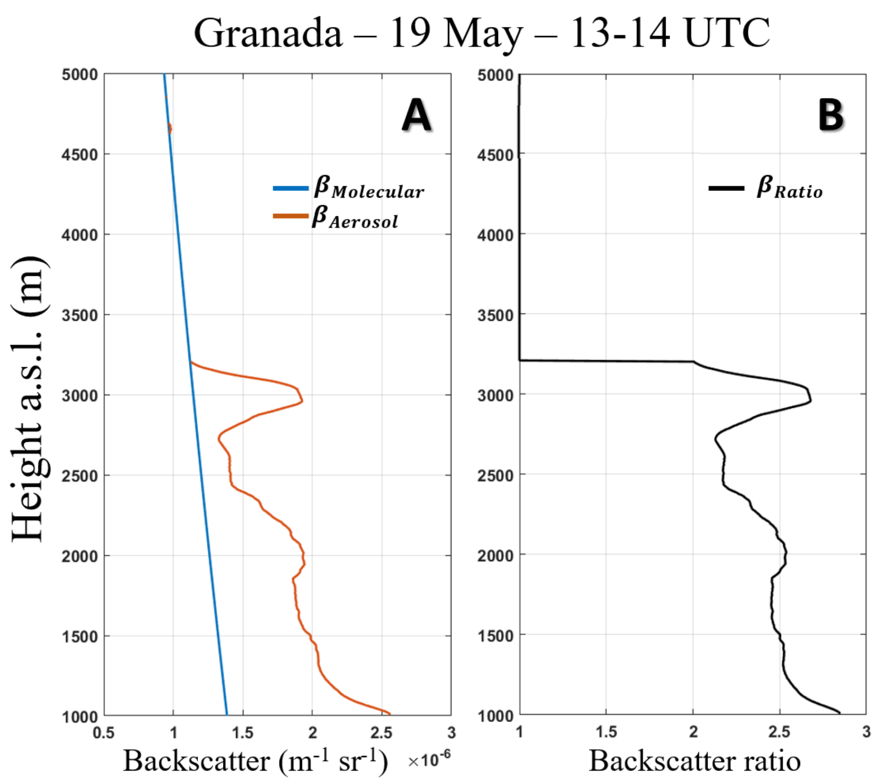

Figure 10 – (A) $\beta_{Molecular}$ (blue line) and $\beta_{Aerosol}$ (orange line). (B) β_{Ratio} (black line). All profiles were obtained from the 532 nm lidar signal

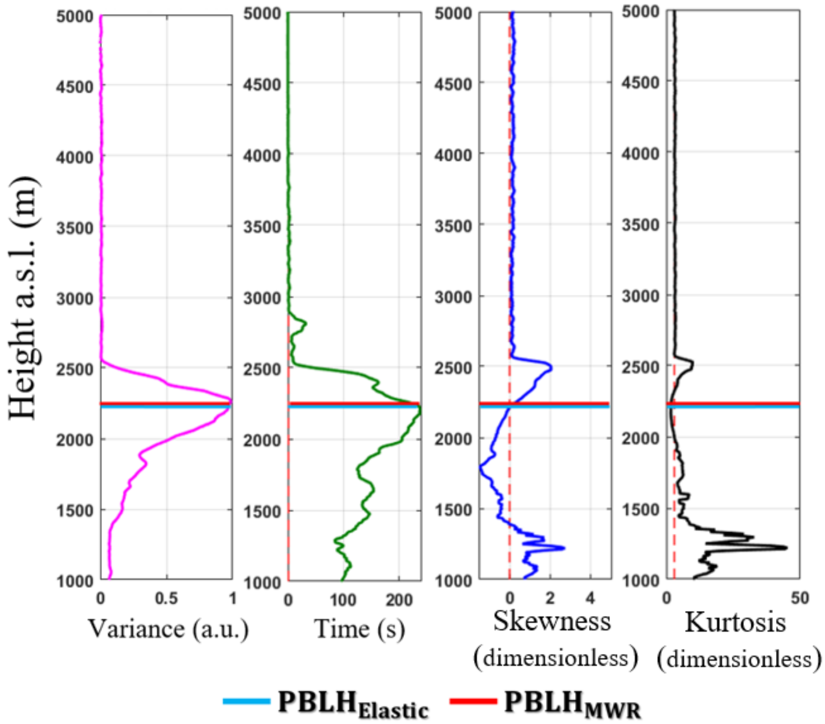

Figure 11 – Statistical moments obtained from elastic lidar data at 13 to 14 UTC - 19 May 2016. From left to right: variance [$\boldsymbol{\sigma}^2_{RCS'}$], integral time scale [$\boldsymbol{\tau}_{RCS'}$], skewness [$\boldsymbol{S}_{RCS'}$] and kurtosis [$\boldsymbol{K}_{RCS'}$].

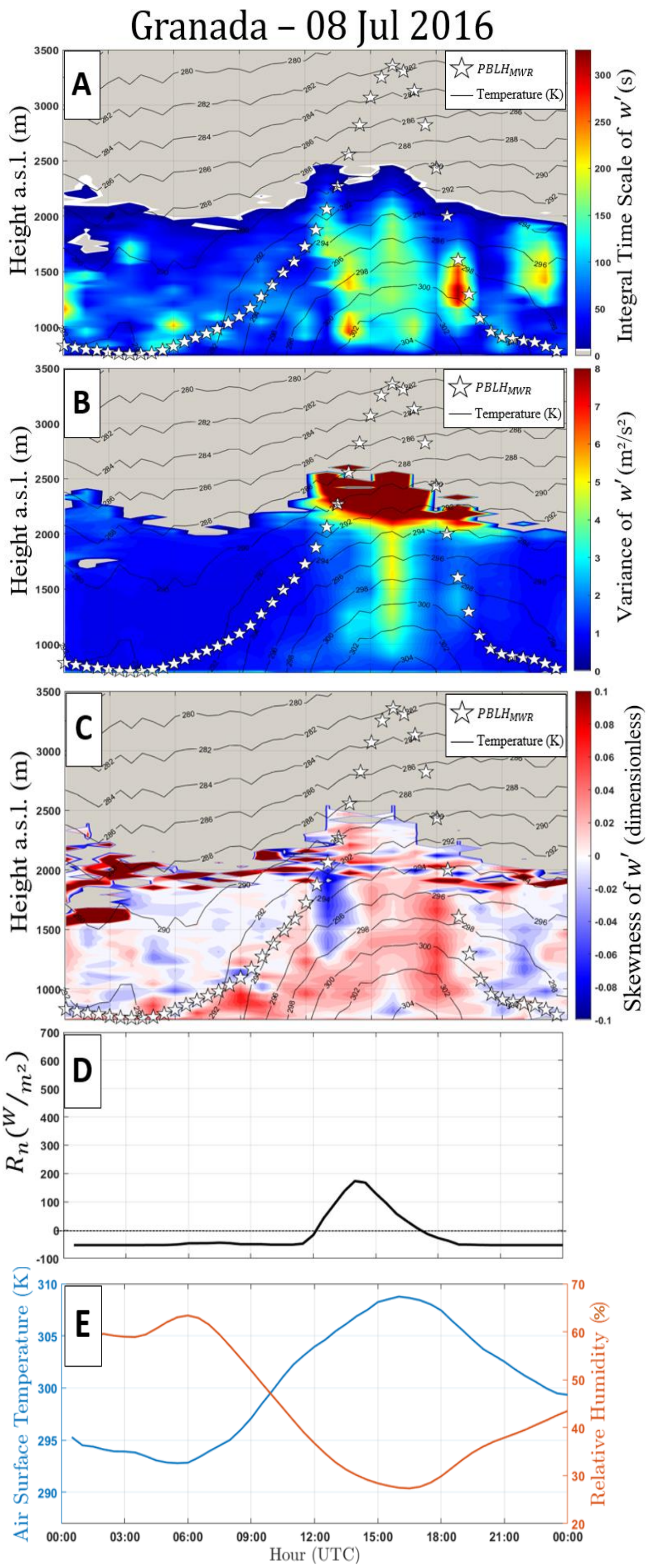

Figure 12 - A – integral time scale [$\boldsymbol{\tau_{w'}}$], B – variance [$\boldsymbol{\sigma}^2_{w'}$], C – skewness [$\boldsymbol{S_{w'}}$], D – net radiation [$R_n$], E – Air surface temperature [blue line] and surface relative humidity [RH – orange line]. In A, B and C black lines and white stars represent air temperature and $PBLH_{MWR}$, respectively.

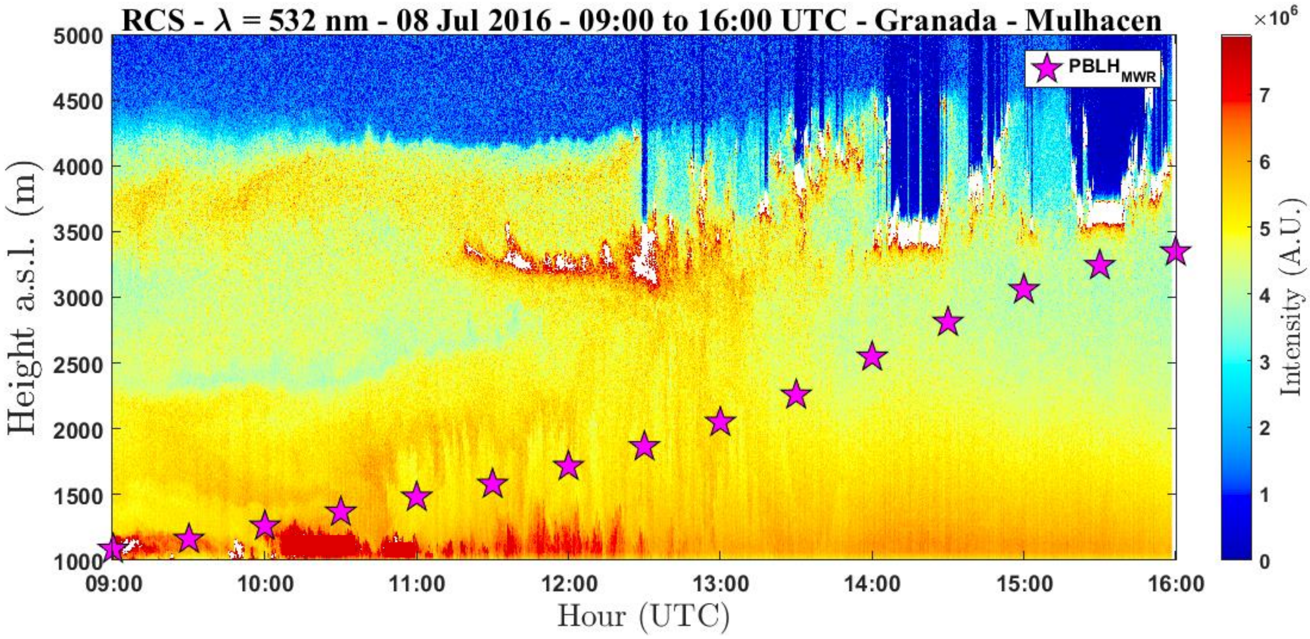

Figure 13 – Time-Height plot of RCS - 08 July 2016. Pink stars represent $PBLH_{MWR}$.

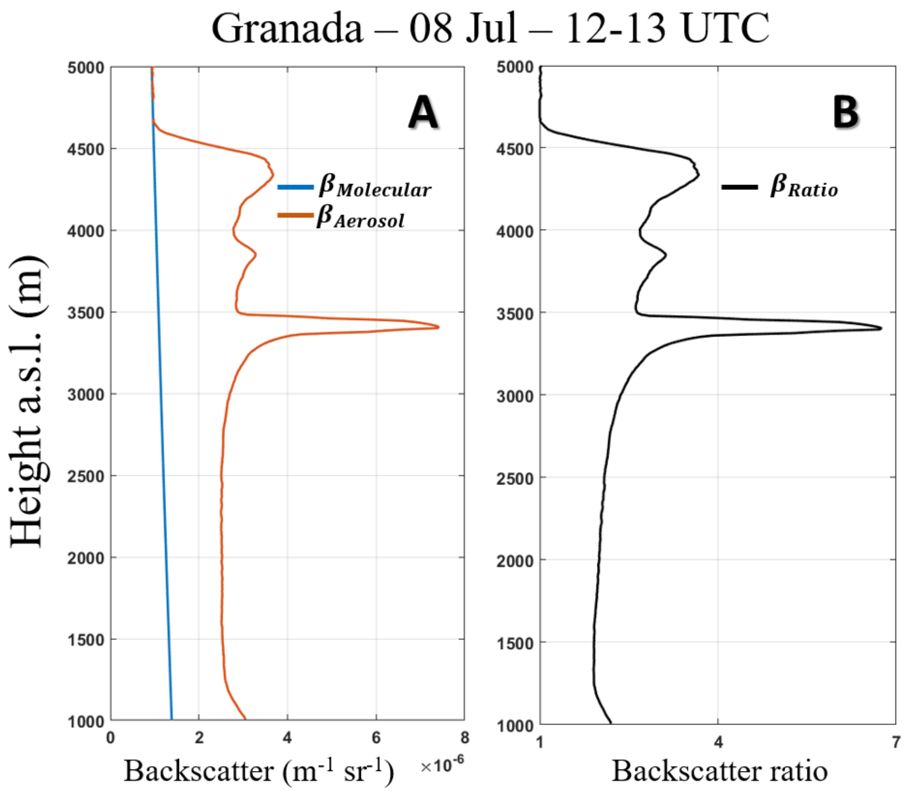

Figure 14 – (A) $\beta_{Molecular}$ (blue line) and $\beta_{Aerosol}$ (orange line). (B) β_{Ratio} (black line). All profiles were obtained from the 532 nm lidar signal

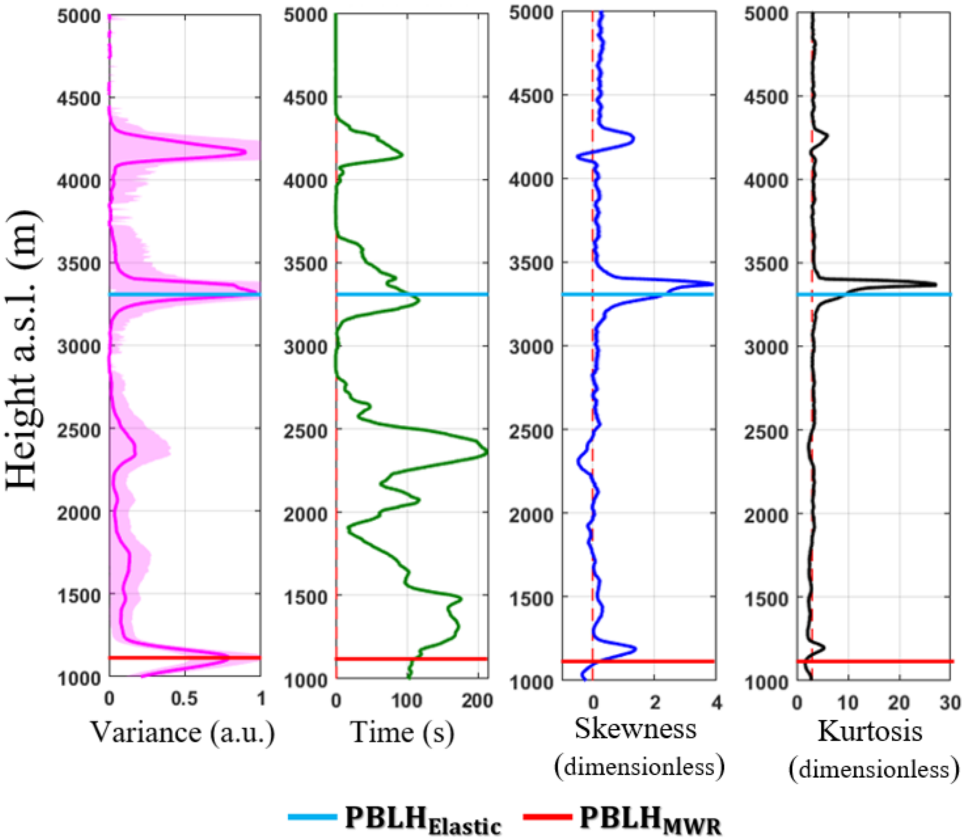

Figure 15 - Statistical moments obtained from elastic lidar data at 11 to 12 UTC - 08 July 2016. From left to right: variance [$\sigma^2_{RCS'}$], integral time scale [$\tau_{RCS'}$], skewness [$S_{RCS'}$] and kurtosis [$K_{RCS'}$].

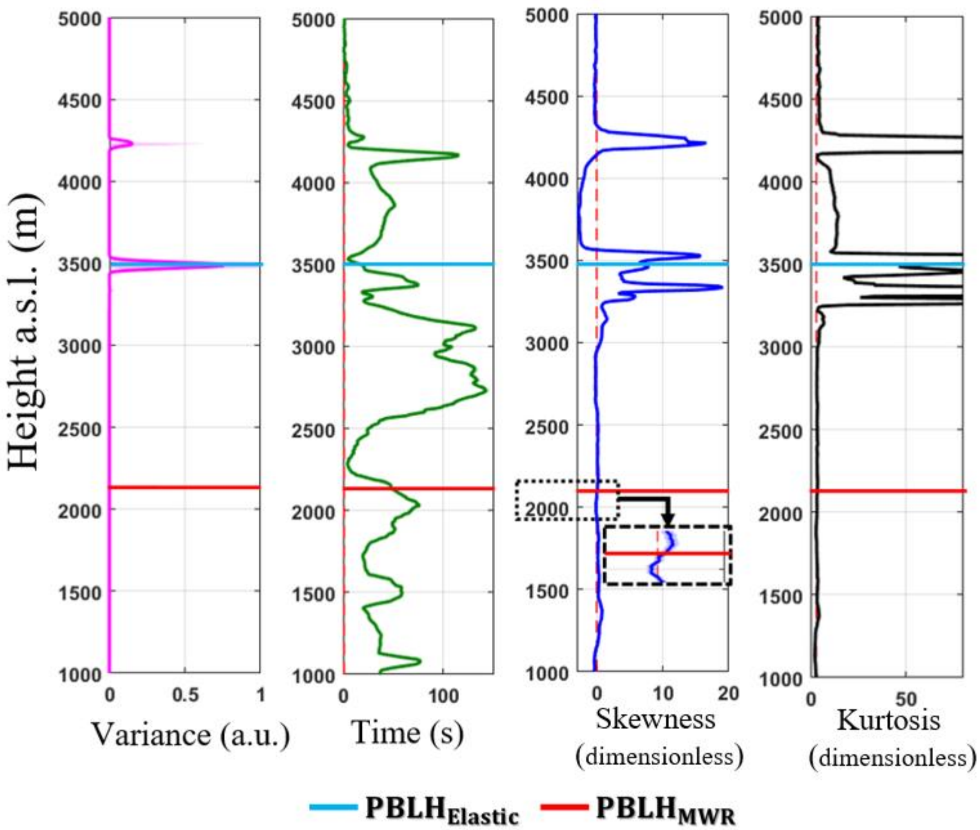

Figure 16 - Statistical moments obtained from elastic lidar data at 12 to 13 UTC - 08 July 2016. From left to right: variance [$\sigma^2_{RCS'}$], integral time scale [$\tau_{RCS'}$], skewness [$S_{RCS'}$] and kurtosis [$K_{RCS'}$].