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## Reply on RC1

Azucena Román-de la Sancha et al.

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Author comment on "Modelling the sequential earthquake–tsunami response of coastal road embankment infrastructure" by Azucena Román-de la Sancha et al., Nat. Hazards Earth Syst. Sci. Discuss., <https://doi.org/10.5194/nhess-2021-381-AC1>, 2022

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### Specific Comments:

**1.- Introduction – this section needs revision, clarification and the inclusion of some recent publications related to lifelines (e.g. the work of J. Williams, 2019, 2020 related to the tsunami vulnerability of critical Infrastructures, etc.) and geotechnics (e.g. the work of Rossetto, T., Goda, K., & De Risi, R., etc...). In this section (at the end of page 2) the models referred to the infrastructure and its interaction with the soil are mixed and needs revision.**

AC: The introduction section was revised, and the following recent references were included:

Williams, J. H., Wilson T.M., Horspool N., Lane E.M., Hughes M.W., Davies T., Le L., Scheele F.: Tsunami impact assessment: development of vulnerability matrix for critical infrastructure and application to Christchurch, New Zealand, Natural Hazards, 96, 1167-1211, <https://doi.org/10.21203/rs.3.rs-1104603/v1>

Goda, K. (2021). Multi-hazard parametric catastrophe bond trigger design for subduction earthquakes and tsunamis. *Earthquake Spectra*, 37(3), 1827-1848.

Goda, K., De Risi, R., De Luca, F., Muhammad, A., Yasuda, T., & Mori, N. (2021). Multi-hazard earthquake-tsunami loss estimation of Kuroshio Town, Kochi Prefecture, Japan considering the Nankai-Tonankai megathrust rupture scenarios. *International Journal of Disaster Risk Reduction*, 54, 102050.

Goda, K., Petrone, C., De Risi, R., & Rossetto, T. (2017). Stochastic coupled simulation of strong motion and tsunami for the 2011 Tohoku, Japan earthquake. *Stochastic Environmental Research and Risk Assessment*, 31(9), 2337-2355.

**2.- In the different models developed in this study, the software used should be clearly identified and the references added. The models adopted for the soil should be detailed defined.**

AC: The following paragraphs were included to enhance the model description:

*Site response model*

“To simulate wave propagation during the earthquake, the selected acceleration history (N90E) was deconvolved using the soil profile of site S4 (Figure 6), using the code SHAKE (Schnabel et al., 1972), which determines the vertical propagation of shear waves in a horizontally stratified semi-infinite soil deposit. Subsequently, the deconvolved earthquake was propagated again upward to verify that the propagation of the deconvolved and the recorded history are consistent. Figure 11 presents the comparison between the recorded and calculated response spectrum.”

#### *Soil dynamic model:*

“The seismic response of the embankment was evaluated using a three-dimensional finite difference simulation. This was carried out using the Finn (1970) constitutive model for liquefiable soils, available in the software FLAC<sup>3D</sup> for the site response analyses of the slope, and to account for soil nonlinearities and loss of strength associated with pore pressure generation during cyclic loading Figure 15. For monotonic loading, an elastoplastic Mohr-Coulomb failure criterion was used that enables horizontal and vertical accelerations, displacements, shear forces and pore pressure to be obtained. The model was composed of 13,632 elements and 16,083 nodes. The dimension of the element was selected based on the geometry and thicknesses of the soil layers. However, numerical distortion of the propagating wave can occur in a dynamic analysis as a result of the modelling conditions, (Itasca Consulting Group, 2009). To represent wave transmission accurately, Kuhlemeyer & Lysmer (1973) suggest keeping the size of the spatial element,  $\Delta l$ , less than one-fifth of the wavelength associated with the highest frequency component of the input wave that contains significant energy,  $f_{max}$  (i.e.  $\Delta l \leq \lambda/5$ ), where the shortest wavelength  $\lambda$  is obtained from  $\lambda = V_s / f_{max}$ . In the case study, the smallest average shear wave velocity  $V_s$  of the site corresponds to that of the first stiff soil layer (i.e. shear wave velocity is around 260 m/s in the first 10 m layer), while the highest excitation at which the energy is concentrated is about 1-5 Hz. Then,  $\lambda$  varies between 260 and 52 m approximately. The maximum spectral responses of the excitation occur even at higher frequencies (i.e. 0.5 and 10 Hz) as shown in Figure 16. Hence, a  $\Delta l$  of 2 m was deemed appropriate. In previous research, using equivalent linear properties (Mayoral et al. 2017; Mayoral et al. 2016; Mayoral et al. 2015), meshes with element sizes of 2 m showed good agreement between finite difference models developed with FLAC<sup>3D</sup> and SHAKE”

#### *Wave propagation model:*

“The tsunami simulation was carried out using the model implemented in the GeoClaw code (Berger et al., 2011), which is based on solving the non-linear shallow water equations through the numerical method of finite volumes, using adaptive mesh refinement to model small-scale features of the bathymetry as well as structures and coastal elements on a scale of meters (LeVeque 2011). The shallow water equations are the standard model used for transoceanic tsunami propagation as well as for local inundation: e.g., Yeh, Liu, Briggs and Synolakis (1994) and Titov and Synolakis (1995, 1998). In one space dimension these are:

where  $g$  is the gravitational constant,  $h(x, t)$  is the fluid depth,  $u(x, t)$  is the vertically averaged horizontal fluid velocity. The function  $B(x)$  is the bottom surface elevation relative to mean sea level. Where  $B < 0$  this corresponds to submarine bathymetry and where  $B > 0$  to topography. GeoClaw code implementation allows the bathymetry and topography to be time-dependent by solving the two-dimensional shallow water equations (LeVeque 2011):

where  $u(x, y, t)$  and  $v(x, y, t)$  are the depth-averaged velocities in the two horizontal directions,  $B(x, y, t)$  is the topography.

The bathymetric and topographic information used was obtained from the GEBCO database, with a resolution of 15 arc seconds. A mesh of 129,600 cells was used, applying 3 levels for mesh refinement, with the finest grids used near the embankment segment, where the grid resolution was 210 m. Considering the characteristics of the fault mechanism of the 1995 Manzanillo earthquake, Table 9, the (Okada, 1995) fault model was used to estimate the vertical displacement on the seabed caused by the seismic event.

Based on the calculated deformations and the characteristics of the earthquake, a tsunami-wave propagation model was run for a simulation period of 1 hour, beginning 15 minutes after the start of the earthquake. Figure 23 shows the simulation results for 1 min. A one-hour simulation period was found for the case study analysed according to records of the duration of the event regarding the wave arriving times (García et al. 1997; Borrero et al. 1997). However, for other cases, longer simulation times could be considered, such as those recommended by ASCE (Robertson, 2017). The authors acknowledge that the grid resolution of the propagation model is a possible research topic for the future. However, a higher resolution was not possible at the time the model was developed. The improvement in the grid spacing would help to reduce uncertainties in the expected flood elevations."

#### *Hydrodynamic model:*

"The hydrodynamic conditions of the simulation reproduce the flow velocities and elevation of the free sea surface of indicator 5, the closest to the coast (Figure 26). The SPH model used is DualSPHysics, which has been widely used for hydrodynamic forces and to model complex fluid flows (González-Cao et al., 2019; Ye et al., 2019)"

"A simulation resolution analysis was performed for the SPH model. The resolution used was the initial size of the lattice nodes of the fluid particles and the fixed particles, defined as inter-particle spacing ( $dp$ ). The simulation was made through tests with 5 different inter-particle spacings, to obtain the resolution that allows a convergence in the results with a lower computational cost (run time).

The hydrodynamic pressures at the position  $x = 10$  m  $z = 2.1$  m of the different resolutions ( $dp = 0.1$  m,  $0.2$  m,  $0.3$  m,  $0.4$  m,  $0.5$  m,  $0.6$  m and  $0.7$  m) were compared. The agreement of the results obtained with different resolutions is quantified taking as reference the data series of the finest resolution of  $dp = 0.1$  m, by means of the normalized standard deviation ( $\sigma$ ), the centered root-mean-square difference ( $\sigma_c$ ), and the correlation ( $R$ ), as shown in the Taylor diagram of Figure 29 (as applied in González-Cao et al. 2019 and Klapp et al. 2020).

Details of resolution, run time and number of simulated particles are shown in Figure 30. The parameters and main characteristics of the simulations are shown in Table 12. The simulations were run on NVIDIA 1650 GPU.

The results of the inter-particle spacing sensitivity analysis show that for all resolutions the correlation is greater than 95% and that improves when the resolution is finer. However, a resolution greater than 0.1 m may not significantly improve the convergence of the results and may increase the computation time. Therefore, a resolution of 0.1 m with a particle number of 104,825 and a computation time of 0.94 h was selected."

### **Section 3.4 "Step 2: simulation of tsunami and wave propagation":**

**3.- Page 302-303: GEBCO is not a project of NOAA; this sentence needs revision.**

AC: Line was revised and modified.

“The bathymetric and topographic information used was obtained from the GEBCO database, with a resolution of 15 arc seconds ”

**4.- The grid for the simulation considers the displacements presented in previous section. In lines 289-290 it is referred “Important vertical displacements of the soil were observed, as well as a tendency of lateral displacement of the body of the slope, increasing with depth.”**

AC: Earthquake induced displacements are considered in the last stage of the modelling framework, the analysis considers the accumulated deformation state of the embankment. This is done by applying the wave-induced hydrodynamic loads to the embankment deformed state. Lines 289-290 refers to earthquake-induced displacements.

**5.- Line 303: a grid with 15 arc seconds (about 300m grid spacing) is not enough to model the flood phase of the tsunami.**

AC: The tsunami simulation was carried out using the model implemented in the GeoClaw code (Berger et al., 2011), which is based on solving the non-linear shallow water equations through the numerical method of finite volumes using adaptative mesh refinement to model small-scale features of the bathymetry as well as structures and coastal elements on a scale of meters. A mesh of 129,600 cells was used, applying 3 levels for mesh refinement, with the finest grids used near the embankment segment, where the grid resolution was 210 m. The authors acknowledge that the grid resolution of the propagation model is a possible research topic for the future. However, a higher resolution was not possible at the time the model was developed. The improvement in the grid spacing would help to reduce uncertainties in the expected flood elevations.

**6.- Line 309: One hour of simulation is not sufficient. The authors should check the recommendations in ASCE 7-16.**

AC: The authors consider that a practical estimation of the combined effect can be obtained from a shorter simulation time for the specific event analysed. A one-hour simulation period was found for the case study analysed according to records of the duration of the event regarding the wave arriving times (García et al. 1997; Borrero et al. 1997). However, for other cases, longer simulation times could be considered, such as those recommended by ASCE (Robertson, 2017). The authors acknowledge that the grid resolution of the propagation model is a possible research topic for the future. However, a higher resolution was not possible at the time the model was developed. The improvement in the grid spacing would help to reduce uncertainties in the expected flood elevations.

The following paragraph was included:

“Based on the calculated deformations and the characteristics of the earthquake, a tsunami-wave propagation model was run for a simulation period of 1 hour, beginning 15 minutes after the start of the earthquake. Figure 23 shows the simulation results for 1 min. A one-hour simulation period was found for the case study analysed according to records of the duration of the event regarding the wave arriving times (García et al. 1997; Borrero et al. 1997). However, for other cases, longer simulation times could be considered, such as those recommended by ASCE (Robertson, 2017). The authors acknowledge that the grid resolution of the propagation model is a possible research topic for the future. However, a higher resolution was not possible at the time the model was developed. The improvement in the grid spacing would help to reduce uncertainties in the

expected flood elevations.”

**7.- In this study, if the effect is to be considered as cascade, the variables over time have to account for the cumulative effect in the numerical models.**

AC: This is correct. This four-stage analysis considers the cumulative effect by modelling both phenomena sequentially. The fourth stage of the analysis considers the accumulated deformation state of the embankment, obtained from the previous stages. The wave-induced hydrodynamic forces are applied to the embankment deformed state. The three analytical approaches are applied dynamically, considering accurately the duration of ground shaking, cyclic loading, pore pressure evolution, wave propagation from the source to the coast and hydrodynamic loading to the embankment. A time-scale diagram was added to clarify the modelling sequence.

**8.- In this work, to evaluate the effect of the tsunami in the infrastructure it is necessary to consider the hydrodynamics variables: height and velocity of propagation of the wave.**

AC: Both hydrodynamics variables: height and velocity of propagation of the wave were considered in the model. The hydrodynamic conditions of the simulation reproduce the flow velocities and elevation of the free sea surface of indicator 5, the closest to the coast. The SPH model used is DualSPHysics, which has been widely used for hydrodynamic forces and to model complex fluid flows (González-Cao et al., 2019; Ye et al., 2019). The validation process was included.

**9.- Figures 24 and 25 need improvement and clarification.**

AC: Figures were modified for clarification.

**Section 3.5 “Step 3: earthquake-tsunami response”:**

**10.-The smooth particle hydrodynamics approach (sph) is highly sensitive to the numerical parameters. The smooth particle hydrodynamics approach (sph) is highly sensitive to the numerical parameters. Using this approach without a convergence study, without a validation, is assuming that any output is possible. Moreover, characterize the pressure with sph is still more challenging. Some validation is required in order to obtain reliable results.**

AC: The SPH model validation was added using the experimental and numerical model of St Germain (2012). The following paragraphs were added:

“To validate the numerical approach, the experimental and numerical model of St Germain (2012) was reproduced, comparing water elevations of the incident wave in two control gauges. A tank 13.17 m long, 2.7 m wide, divided into two sections, and is 1.4 m in height (Figure 27) was considered. The model is made up of a dambreak, consisting of a block of water of 0.85 m height, that is released at time 0 through a swinging gate to travel towards the outflow.

The validation SPH simulation parameters are shown in Table 11.

Table 11 Parameters and main characteristics of the SPH simulation

Parameters	Value
Kernel Function	Wendland
Time-step	Algorithm Verlet
Viscosity Artificial	$\alpha=0.01$
Inter-particle spacing (m)	0.03
Number of particles	545,929
Simulated time (s)	10
Time out (s)	0.1
Computing time (h)	0.35

The simulation results are water heights at points W1 and W2 (Figure 28). The standard deviation of the DualSPHysics model with respect to the experimental model is 5.4 cm for W1, and 5.2 cm for W2, which are 6.38% and 6.16% with reference to the initial height of the water. The standard deviation of DualSPHysics with respect to the numerical model of St Germain et al. is 2.9 cm for W1, and 3.5cm for W2, 3.4% and 4.1% concerning the initial height of the water.

#### Analysis of inter-particle spacing sensitivity

A simulation resolution analysis was performed for the SPH model. The resolution used

was the initial size of the lattice nodes of the fluid particles and the fixed particles, defined as inter-particle spacing ( $dp$ ). The simulation was made through tests with 5 different inter-particle spacings, to obtain the resolution that allows a convergence in the results with a lower computational cost (run time).

The hydrodynamic pressures at the position  $x = 10 \text{ m}$   $z = 2.1 \text{ m}$  of the different resolutions ( $dp = 0.1 \text{ m}$ ,  $0.2 \text{ m}$ ,  $0.3 \text{ m}$ ,  $0.4 \text{ m}$ ,  $0.5 \text{ m}$ ,  $0.6 \text{ m}$  and  $0.7 \text{ m}$ ) were compared. The agreement of the results obtained with different resolutions is quantified taking as reference the data series of the finest resolution of  $dp = 0.1 \text{ m}$ , by means of the normalized standard deviation ( $\sigma$ ), the centered root-mean-square difference ( $\sigma_c$ ), and the correlation ( $R$ ), as shown in the Taylor diagram of Figure 29 (as applied in González-Cao et al. 2019 and Klapp et al. 2020).

Details of resolution, run time and number of simulated particles are shown in Figure 30. The parameters and main characteristics of the simulations are shown in Table 12. The simulations were run on NVIDIA 1650 GPU.

Table 12 Parameters and main characteristics of the SPH simulation

Parameters	Value
Kernel Function	Wendland
Time-step	Algorithm Symplectic
Viscosity Artificial	$\alpha=0.01$
Inter-particle spacing (m)	0.1
Number of particles	104,825
Simulated time (s)	90

Time out (s) 0.1

Computing time (h) 0.94

The results of the interparticle spacing sensitivity analysis show that for all resolutions the correlation is greater than 95% and that improves when the resolution is finer. However, a resolution greater than 0.1 m may not significantly improve the convergence of the results and may increase the computation time. Therefore, a resolution of 0.1 m with a particle number of 104,825 and a computation time of 0.94 h was selected.”

**11.- How the soil was modelled should be clearly defined.**

AC: The embankment and soil were modelled using the same three-dimensional analysis of stage one, starting from the deformed state model obtained. Wave arrival and interaction with the soil and embankment was analysed applying the resulting vertical and horizontal components of hydrodynamic loads in the corresponding elements of the sand slope and the embankment faces. Loading was applied incrementally, until the steady state of each point was reached, in an overall 1.5 min period.

Please also note the supplement to this comment:

<https://nhess.copernicus.org/preprints/nhess-2021-381/nhess-2021-381-AC1-supplement.pdf>