Response to review of Daniele Pedretti
Erwin Zehe et al.


We sincerely Daniele Pedretti (DP) for his thorough and thoughtful assessment of our manuscript.

DP: The manuscript ("Preferential Pathways for Fluid and Solutes in Heterogeneous Groundwater Systems: Self-Organization, Entropy, Work") provides a new framework that combines the use of free energy and entropy to characterize and quantify the emergence of preferential flow and channelled transport in heterogeneous media. Although the specific components of this framework are not novel themselves, as correctly acknowledged by the authors, their combined use makes it a novel way that help disentangling open questions regarding the mechanisms of transport in heterogenous porous media. The paper is well written. The objective, methodologies and conclusions are clear. I have summarized a line-by-line set of comments for the authors, which makes me recommending me accepting this manuscript after major revisions.

RESPONSE: We thank the reviewer for the positive comments.

DP: My major concern is that, while I consider this approach excellently explained, it should have been demonstrated on a 3D heterogeneous system. Percolation thresholds are different in 2D and 3D systems. As such, the results of this study could have been very different if drawn from 2D or 3D stochastic models. I ask the authors to at least comment on this issue critically in their manuscript.

RESPONSE: We agree that a transfer of the proposed assessment to a three 3D stochastic media would yield interesting insights, which will for sure differ somewhat from what we found in 2D. However, we respectfully disagree that this might imply a different qualitatively behavior, as long as we work in a confined system (no flow boundary conditions for the upper, lower, inlet and outlet boundaries). The local changes in power arise from the local feedback on the pressure head gradient in front of the low conductivity bottlenecks. Gradients steepen ahead of the bottlenecks, which implies a higher power, locally. This feedback will also occur in a 3D confined system, as it is a direct result of the boundary conditions. It would not likely occur in an aquifer with a free surface neither in 2D or 3D. In the revised manuscript we will state that an analysis in 3 D is the next step of a forthcoming study, and explain why think that we expect qualitatively similar results due to the above stated reasons.
We furthermore like to stress, that percolation considerations are not relevant here, as
the domains are well connected and well above a percolation threshold. Moreover, the
original study by Edery et al. (2014), which we cite, presented already a critical path
analysis in reference to the percolation threshold, based on the common assumption
that preferential flows are a manifestation of percolation, controlled by the lower cut-
off for the hydraulic conductivity from which a path is possible. The limitations of
percolation theory in evaluating the preferential flow are presented therein, and as
such, the equivalence or connection between percolation and entropy is not
straightforward.

**DP:** Thanking the authors for considering our 2017 WRR publication, I also suggest
having a look at our follow-up manuscript (Bianchi and Pedretti 2018 WRR
https://doi.org/10.1029/2018WR022827) where we extend our previous theory by
computing the geological entrogram on evolving sampling scales. I think that most
conclusions we got in those studies there are very much in line with those obtained
through this study. Indeed, in the 2018 paper we also address the question of 2D vs 3D
models, and described at page 4444 how solute particles tend to sample specific K
clusters when travelling in the heterogeneous media.

**RESPONSE:** We will be pleased to read your 2018 paper and refer to the study and
conclusions in our revised manuscript, if/where appropriate.

Best Regards

Daniele Pedretti

University of Milan - UNIMI (Italy).

Line-specific comments

**DP:** L72-76 I wouldn't be so strict. Someone has succeeded in this task (Zhang et al
2013 JH for instance). What is really complicated is finding a universal way to predict
solute transport based on the aquifers geological structures. In Bianchi and Pedretti’s
works on geological entropy we found an explanation for that: the lower the structure’s
Shannon entropy, the more organized the flow and transport patterns in the field. In
that set of works our aim was to start from the geology and not from self-customed
flow fields (e.g. power-law distributed seepage velocities).

**RESPONSE:** We thank DP for pointing this out, and will revise this passage to be less
strict.

**DP:** L97 "the probability of solutes to pass through HIGH (not low) conductivity regions".
Please, fix it.

**RESPONSE:** We will fix this; thanks for noting the typo.

**DP:** L98 Please consider also our follow-up study (Bianchi and Pedretti 2018 WRR),
where we study evolving scales of geological entropy rather than studying fixed-size
blocks (as we did in the 2017 paper). In the 2018 paper we developed the concept of
entrogram scale, which is also nicely correlated with the emergence of preferential flow
and solute channelling.

**RESPONSE:** We will be pleased to read your 2018 paper and refer to the study and
conclusions in our revised manuscript, if/where appropriate.

**DP:** L101 enigmatic OK, emergent not really I would say.

**RESPONSE:** Agreed. We will delete the term emergent.
Again, I wouldn’t be so strict ("virtually impossible"). I’d rather just say that such predictions remain challenging. For instance, Bianchi and Pedretti works or Zhang et al 2013 showed that it can be done. There is also a set of works by Rizzo and de Barros showing that predictions can be made starting from the aquifer structures.

Agreed. We will revise this passage accordingly. We note, too, that we can also achieve useful predictions of preferential transport of solutes in the partially saturated zone, in cases where detailed information about the pdf of macropores in soil and their connectivity are available.

please see comment at L98.

As for the L98 comment, we will read your 2018 paper and refer to the study and conclusions in our revised manuscript, if/where appropriate.

Rather than Objectives, these are Results and Conclusions.

We agree that we provide here some foreshadowing on the results. The idea is to interest and motivate the reader to study, in particular, the theory section. In the revised manuscript, from the end of line 164 ("Specifically"), we will define the text as a new paragraph.

I wonder if all these nice concepts can be exported directly to 3D models, considering the different percolation thresholds between 2D and 3D models. Could the authors discuss on this?

We think that the above mentioned local feedback on the head gradient will also occur in a 3D confined system. As such we expect qualitatively similar behavior in three 3D, as noted in our response to the second comment above. In the revised manuscript, we will include a brief consideration of these comments/responses in the conclusion and outlook section.

why no local dispersion? This is a physical mechanism, which can substantially modify the solute pathways by increasing mixing and coalescence among the so-called "lamellas". Why neglecting it? I think this should have been investigated, from low to high Peclet numbers.

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as the "lamella" description of solute transport in heterogeneous media (e.g. https://doi.org/10.1017/jfm.2015.117) which also strongly depends on concentration gradients transversal to the main flow directions? or the concepts of "least-resistance paths" (e.g. https://doi.org/10.1002/2017WR020418)?

**RESPONSE:** We think these concepts are well connected. At the end of the day, an increase in spatial organization implies a steeper gradient. There are many ways to express this, but there is only one mechanism to explain why this implies ordering and this is the second law of thermodynamics. This is because production of physical entropy implies essentially to deplete gradients.

**DP:** L403-405 this looks like a conclusion of this work, rather than a result. Consider moving it to the appropriate sections

**RESPONSE:** Indeed we do a little bit of foreshadowing here, but we think this is helpful to keep the reader on track. We state clearly that "In the following, we demonstrate".

**DP:** L442 this is very similar to a conclusion by Bianchi and Pedretti 2018 (page 4444), which reads "These observations are further confirmed by the CDFs of the subsamples of K values, which show a significantly higher variability for 2-D fields compared to 3-D (Figures 6c and 6d). These results strengthen the knowledge that solutes tend to travel in the upper 15–20% of the K distribution (K classes 32–40 in Figure 6), which tend to fully percolate in 3-D correlated random fields regardless of their overall structure (Fogg et al., 2000; Fogg & Zhang, 2016; Harter, 2005). " Consider commenting on that

**RESPONSE:** We will happily include this point in our discussion here.

**DP:** L457 I find it a bit complicated to relate "watts" to something related to groundwater. I mean, the entire derivation of power is clearly described in the previous sections, but as a hydrogeologist I have some problem to understand, for instance, if this is a high/low power. For instance would 2 watts be a high or lower power in this context?

**RESPONSE:** We absolutely agree that power and W/m is not very common groundwater and vadose zone hydrology. Zehe et al. (2013) analyzed energy conversion associated with infiltration and found that macropores increase power in the infiltrating water flux. The maximum values during a rainfall event were of order 2 W/m². The use of W/m² is much more common when dealing with the landsurface energy balance, as evaporation as water flux can be expressed as energy flux as well. In this context it is interesting to recall that the climatological land-surface energy balance is of order 100 W/m². By comparison, a difference of 2 W/m² is hence quite significant. In the revised manuscript, we will add text to include this background information, and comment on the significance of a 2 W per unit width increase as noted on L457.

**DP:** L455-478: these are great findings. It is particularly interesting that at some point the system behaves effectively as a 1D system. I'm wondering if they also hold for a 3D system, which is in general more percolated than a 2D one.

**RESPONSE:** Thanks. You raise a very good point. We expect that the 3D system will deviate even more from the 1D approximation, but the local feedback on the head gradient will remain in a confined aquifer. As mentioned above, we will address this point in the conclusions and outlook section of the revised manuscript.

**DP:** L487-488 for the same token, then solute injection mode (i.e resident vs flux-averaged) could be also important to control the "effective" system power, right? Even if the flow field is the same, you change the way particles are already injected into certain
flow zones.

**RESPONSE:** Good point, thanks. We will mention this in the revised manuscript.

**DP:** L505-507 this is well aligned with the result of Bianchi and Pedretti 2017, 2018, who expressed geological entropy with the BTC moments.

**RESPONSE:** Agreed. We will mention this in the revised manuscript.

**DP:** L537 also similar to Bianchi and Pedretti 2017, 2018.

**RESPONSE:** Agreed, see reply to the previous comment.

**DP:** L558 notice an underlined word: just a writing typo?

**RESPONSE:** Indeed, we will fix this.

**DP:** L564 and the 2018 work, which extends the previous one.

**RESPONSE:** Yes, we will read this work and refer to it where appropriate.

**DP:** L571 I agree that the CTWR beta could be a good indicator to connect to entropy. In general, any indicator that explains the departure from the BTC symmetry could be also good. This is why in Bianchi and Pedretti 2017, 2018 we did not fit a power-law curve to our BTCs, but limited ourselves to the third moment of the BTC, which is strongly correlated with geological entropy indicators. However, in Pedretti and Bianchi 2018 ADWR (https://doi.org/10.1016/j.advwatres.2018.01.023) we found that for a system with very-low geological entropy (i.e. high spatial order) all BTC tailing tended to the same power-law value, close to one. Any comment on that?

**RESPONSE:** We agree that various measures of non-symmetry in the BTC may act as good measures of non-Fickian transport. Zehe and Flühler (2001), for example, used also the skewness of vertical travel distance as a measure of preferential flow in infiltration patterns. In fact, one could also use, for example, the difference in the entropies of the actual BTC and the (homogeneous case) Fickian BTC. However, these additional comments are beyond the focus of our current study.

**DP:** L604 I think it could have been worth looking at the probability of transitioning of a particle from a low to a high flow zone, and relate it to the derived power P.

**RESPONSE:** This is certainly an interesting point, but beyond the scope of the current study. We plan to explore this and related aspects in a future study.

**DP:** L606-608 to me the framework should be also demonstrated on a 3D simulated aquifer to properly claim that this approach "holds the keys" to disentangle a problem that have been a great challenge for many researchers until now. I may agree with that, and it would be amazing, but it has to be proved.

**RESPONSE:** We agree that further investigations in 3D are needed, but we also encourage study of systems in which K is evolving. We will modify the text here to note these points, and to express that this approach potentially holds the key.

On behalf of all co-authors I thank Daniele Pedretti again for his helpful comments. 
Best regards, Erwin Zehe

References: