

Geosci. Model Dev. Discuss., author comment AC2  
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## Reply on RC2

Jinyun Tang et al.

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Author comment on "Supporting hierarchical soil biogeochemical modeling: version 2 of the Biogeochemical Transport and Reaction model (BeTR-v2)" by Jinyun Tang et al., Geosci. Model Dev. Discuss., <https://doi.org/10.5194/gmd-2021-310-AC2>, 2022

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**Comment:** This paper describes an updated version of the Biogeochemical Transport and Reaction Model (BeTR-v2) including updated algorithms for reactive transport and numerical coupling with vegetation and hydrological processes. Simulations are conducted with the standalone version of the model and compared to analytical benchmarks, and a version of the model coupled to the E3SM Land Model is used to conduct and evaluate global simulations with alternate numerical implementations of soil biogeochemistry and plant soil coupling. The simulation results compare well with analytical benchmarks. Coupled land model simulations resulted in different carbon, nitrogen, and phosphorus cycle outcomes for the different numerical implementations.

Overall, the manuscript is well written and provides a clear description of the model developments, the simulations that were performed, and the results. There are a few typographical errors and some areas where clarity could be improved.

**Response:** We appreciate the reviewer's positive assessment of our work.

**Comment:** Page 3, Line 3: I would word this "sharing of common process representations..."

**Response:** Done.

**Comment:** Page 3, Line 19-20: ...enable efficient code and knowledge sharING ... improvements that have BEEN brought...

**Response:** Done.

**Comment:** Page 4, line 10: SINCE significant code rewriting...

**Response:** This phrase is now replaced with "that since significant code re-writing and data restructuring have occurred after ELM branched out from CLM4.5".

**Comment:** Equation 1:  $C_g$  is used in the third right-hand-side term (with  $D_s$ ), and I think it should be  $C_s$  instead

**Response:** The typo is now corrected.

**Comment:** Page 5, line 18-19: A bit more description of the solver method would be helpful so readers can get a basic understanding without reading a different paper. Also, does the time stepping method account for truncation errors at longer time steps? Is some adaptive time stepping included for cases where the model time step is too long to resolve fast biogeochemical processes (maybe not important in the simulations presented here but potentially important in some applications such as explicit tracking of oxygen concentrations)?

**Response:** Please also see our response to a similar comment from Reviewer #1, above. For our description of the numerical methods, we revised the text as “Gaseous and aqueous diffusion are solved together using the dual-phase algorithm (that assumes equilibrium between gaseous and aqueous phases) with the implicit time stepping method (Tang and Riley, 2014), which is equally accurate but simpler than the treatment in BeTR-v1 that requires calculating locations of wetting fronts in the soil. Solid phase diffusion is also solved implicitly. Aqueous advection is solved using the mass-conserving semi-Lagrangian approach (Manson and Wallis, 2000), which is more accurate (by reducing numerical dispersion) than the upstream scheme used in BeTR-v1. Biogeochemical reactions are solved using the multiple-flux-co-limiting algorithm (Tang and Riley, 2016), which considers the production and consumption fluxes concurrently, so that there is no delay between nutrient mineralization and its competition by consumption fluxes within a time step, a critical feature to resolve the nutrient limitation dynamics (Tang and Riley, 2018). To ensure numerical accuracy, within each modeling time step of ELM (which is 30 minute), each solver uses the adaptive time stepping that exits when either the relative difference between solutions based on coarse time step and halved time step is less than 0.1% or when the minimum time step (30 seconds) is reached.”

**Comment:** Section 2.4 and Table 1: I had a hard time keeping track of what the differences were between the different simulations. The short descriptions in Table 1 are not very informative because they refer to specific code directories rather than numerical methods, and include several different contrasting numerical approaches described in only one table column. I would suggest adding more columns to the table to clearly differentiate the features of the different implementations. Separate columns could include plant-soil competition solver, plant allocation solver, and parameterization which all varied across different simulations. I would avoid referring to specific code directories where possible and instead refer to the differences in underlying methods, which is more universal. In the text description (page 10), the use of italicized “ecacnp” in some places and the names of the implementations (e.g., ELMv1-ECA) in others is confusing and seems specific to this code base rather than a general description of numerical approaches. I would suggest using only one terminology, or else including the “ecacnp” terminology in Table 1 so it’s easier to keep track of the different terms.

**Response:** By following these suggestions, and those from Reviewer #1, we revised the table by adding more entries to describe the differences among model configurations:

Table 1. Summary of the configurations for the four global simulations.

Model configuration	ELMv1-ECA	ELMv1-ECA-V	ELMv1-BeTR-ECA0	ELMv1-BeTR-ECA
Code base	Default	Default	src/Applications/s oil-farm/v1eca	src/Applications/s oil-farm/v1eca

Soil BGC	Default	Default	Implemented ELMv1-ECA soil BGC in BeTR	Implemented ELMv1-ECA soil BGC in BeTR
Plant carbon and nutrient allocation	Default	Multiple-flux-co- limiting solver	Multiple-flux-co- limiting solver	Multiple-flux-co- limiting solver
Parameters	Default	Default	Default	Recalibrated

**Comment:** Page 10, line 18-19: "Comparing ELMv1-ECA and ELMv1-ECA" - these are both the same. Should one be different?

**Response:** It is corrected as "By comparing ELMv1-ECA-V and ELMv1-ECA".

**Comment:** Figure 2: There was not an explanation of how column integrated heterotrophic respiration, soil surface CO<sub>2</sub> flux, and CO<sub>2</sub> infiltration rate were calculated and what exactly they represent. I assume the surface flux takes transport of gaseous and dissolved CO<sub>2</sub> into account whereas integrated HR is instantaneous production?

**Response:** To address this issue, we revised the caption of Figure 2 as "(a) Heterotrophic CO<sub>2</sub> flux simulated by the 10-cm thick single layer model; (b) column integrated heterotrophic flux (by summing up contributions from all layers in the soil column), soil surface CO<sub>2</sub> flux (from capillary exchange and diffusion considering equilibrium between gaseous and aqueous phases) and CO<sub>2</sub> infiltration flux; (c) evolution of soil CO<sub>2</sub> concentration corresponding to panel (b). "

**Comment:** Figure 3: Why was accelerated spinup used here instead of the normal spinup or historical simulation?

**Response:** We made this choice because, for accelerated spinup, all models started with the same initial conditions. However, when exiting accelerated spinup, there will be a significant increase of the soil organic matter pools (as accelerated spinup means to shorten the time needed for the model to reach equilibrium) through rescaling (based on simulation dependent rescaling factors) of the soil organic matter pools, which further amplifying the model difference (see further discussions in Koven et al. (2013), where the accelerated spinup method was developed). Therefore, using accelerated spinup reduces the aliasing impact resulting from the rescaling factors.

**Comment:** Page 18, line 7-8 and Table 2: I would use the PFT names rather than numbers which are not meaningful to readers to are not closely familiar with this land model

**Response:** We now spelled explicitly the PFT names in the text as PFT-4 (broad leaf

evergreen tropical tree) and PFT-6 (broadleaf deciduous tropical tree). We kept the use of PFT-4 and PFT-6 in the table entries (for formatting purpose as the use of full name will make the table too busy), but do note the PFT names in the table's caption.

**Comment:** Page 18, line 11: "other variables" - Explain which variables

**Response:** We now spelled them explicitly as "(NBP, vegetation carbon, soil carbon, and total ecosystem carbon)".

**Comment:** Table 2: Both columns have the same heading "ELMv1-ECA". One should be ELMv1-BeTR-ECA.

**Response:** This was a typo brought in when we revised the initial submission before discussion. Now it is corrected by identifying "ELMv1-BeTR-ECA" on the right side.

**Comment:** Page 19, line 16-18: This sentence feels oddly judgmental. The previous sentence reports better agreement with some benchmarks but there also seems to be worse agreement with others, so it might be more balanced to say that numerical differences can significantly change model outcomes even without changing the underlying differential equations of a model.

**Response:** We revised the text to address this concern: "This better agreement between ELMv1-BeTR-ECA and some benchmarks suggests that the numerical difference can significantly influence the performance of a supposedly good mathematical representations of ecosystem biogeochemistry."

**Comment:** Page 21, line 3: Estimates of P dynamics also changed, not just N.

**Response:** We revised the sentence as "Therefore, a model calibration using C cycle variables led to very different estimates of N cycle parameters and thereby different nitrogen dynamics and phosphorus dynamics (through N and P co-modulated biogeochemical feedbacks)."

**Comment:** Table 3: The units of the numbers are never described and it's not clear whether a higher number means a better or worse fit to the benchmarks.

**Response:** In the caption of Table 3, we now added "All metrics are normalized to the range from 0 to 1, where greater values indicate better performance."

**Comment:** Page 23, line 12: What is meant specifically by "numerically more robust"?

**Response:** To clarify this issue, we revised the sentence as "We found that because the multiple-flux-co-limiting numerical solver more tightly couples plant and soil processes during nutrient competition (so that it is numerically more robust than the solver used by default ELMv1-ECA model; Tang and Riley (2018, 2016))."

**Comment:** Page 24, line 2: I don't think there is a basis here to decide whether model parameters are "incorrect" or that a particular numerical coupling is "inappropriate." This study shows that different numerical approaches can yield different results. Without a clear demonstration that one approach or the other fails relative to some benchmarks I don't think it can support a declaration that one is right or wrong. A more balanced wording might be that different numerical approaches can significantly change model behavior and that care should be taken to evaluate whether re-parameterization is necessary following numerical changes. This was clearly demonstrated in this study where the land model needed to be recalibrated following a change to the numerical coupling scheme.

**Response:** We modified the tone of the last sentence by using “inappropriate numerical coupling will potentially result in incorrect model parameters that may affect predictions of carbon cycling variables under a changing climate and increasing atmospheric CO<sub>2</sub> concentrations.” We maintain our opinion that a proper numerical approach is essential to obtain numerical solutions that are consistent with the differential equations being solved. In previous papers (Tang and Riley, 2016, 2018), we learned that the solution strategy used by the default ELMv1-ECA model delays the availability of newly mineralized inorganic nutrient for uptake to the next time step, while the multiple-flux-co-limiting solver synchronizes mineralization and uptake as formulated by the governing equations. Therefore, as time step size decreases, the default ELMv1-ECA model will not converge to its governing equations. If we assume that the governing equations are correct, then the default ELMv1-ECA has to make up for this deficiency by using inappropriate parameters. In turn, we may obtain the right answer for wrong model formulations because inappropriate numeric solutions and model calibration together may mask the insufficiency in model formulations, or assert that a correct model formulation is incorrect because the numerical code has to use inappropriate parameter values.