

Ann. Geophys. Discuss., author comment AC2  
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## Reply on RC2

Johann Stamm et al.

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Author comment on "A technique for volumetric incoherent scatter radar analysis" by  
Johann Stamm et al., Ann. Geophys. Discuss.,  
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We thank the referee for the detailed review and comments. We will answer the comments in the order they appear.

We have included most of the referee comments before our answer such that it is easier to see what we are referring to. The referee comments are written in italics.

### Major comments

1.

*> The manuscript does not handle the F-region parallel ion velocities correctly. The momentum equation in Eq. 3 is a vector equation, and it is approximately valid for the two perpendicular components. Nonetheless, this equation is not valid for the parallel component at F-region altitudes. Using that fact that  $v_{\parallel} \times B = 0$  and assuming that  $E_{\parallel}$  is small, the parallel component of Eq. 3 reduces to  $v_{\parallel} = u_{\parallel}$ , implying that the parallel ion velocities are always equal to the parallel neutral velocities. This is generally not true in the F-region. A proper treatment of ion parallel velocity in the F-region requires the inclusion of gravity, ion pressure gradients, and ambipolar electric fields. The ion inertia terms can also become important during times of rapidly varying ion upflow.*

*> In principle, EISCAT 3D measurements could be used to volumetrically reconstruct all three components of the F-region ion velocities, including the spatial variations of the ion upflow velocities. The algorithm presented in this manuscript, however, would fail to do that. This manuscript is not solving for  $v_{\parallel}$ , but instead solving for  $E_{\parallel}$  and  $u_{\parallel}$  assuming the two quantities are related to  $v_{\parallel}$  through an invalid parallel momentum equation.*

*> Figure 8 shows low uncertainties in the vertical neutral wind estimates extending all the way up to 200 km altitude. This is unreasonable since the ion velocities that the radar measures become collisionally decoupled from the neutral velocities at high altitudes, meaning the radar data cannot actually be giving meaningful information on neutral velocities at those altitudes. This unreasonable result is a direct consequence of the invalid parallel momentum equation.*

This study is for showing that it is possible to use multi-beam multi-static ISR measurements to obtain volumetric measurements of electric field and neutral wind in the

ionosphere. In that sense, we did some simplifications of the momentum equation where we neglected the smallest terms, that is advection, gravity and pressure gradients. It is possible to extend the model to include these terms. This will make the model more correct, but also requires even more calculations.

The shown uncertainties do not include those introduced by assumptions or simplifications made. The neglected influence of advection, gravity and pressure gradient terms on the velocities are therefore not reflected as increased uncertainties. Typically, these terms are small, but in the uppermost part of our volume, they can be large enough to become significant. If future work uses field-aligned/vertical estimates of neutral wind or electric field, they will have to consider these terms.

In the revised manuscript, we will state the momentum equation including the terms mentioned above explicitly, before we simplify it to obtain the equation we use in the analysis. We will also clarify that the assumptions and simplifications we did are not included in the shown uncertainties .

2.

*> For vector basis functions, the weights should generally be arrays not scalars. [...] [It is implied that] all three components of the basis function get the same weight, which is an unusual restriction. To allow the three components to vary independently, the coefficients should be allowed to be different for the different vector components [...]*

*> To be general, the three different components of  $\eta$  should be treated as three separate unknowns.*

It appears that the text was confusing since the the three components of the basis functions are allowed to vary independently in the calculations and simulations.

This will be clarified in the revised manuscript.

3.

*> The manuscript does not assume equipotential field lines and does not explain the rationale for allowing large variations in electric fields along a field line. Past E-region neutral wind estimation techniques such as Thayer [1998] and Heinselman and Nicolls [2008] have always asserted that electric fields are invariant along field lines such that F-region measurements of the electric fields can be mapped into the E-region. The mapping of F-region electric fields into the E-region is crucial for all of these past studies of E-region neutral winds using ISR; without that assumption the ion momentum equation is unsolvable in the E-region. Past sounding rocket studies have demonstrated the reality of field line mapping using payloads that can measure electric fields independently of ion velocity [Sangalli et al., 2009].*

*> In this manuscript the a priori standard deviation of the electric field gradient is allowed to be 20 mV/m per 2.5 km in all three directions, including along the field lines. This is equivalent to asserting that field-aligned mapping of the electric fields does not function between the F- and E-regions; fields of 50 mV/m in the F-region at 300 km can change by more than 100% over the distance to the E-region at 100 km.*

*> Ignoring field-aligned mapping of electric fields between the E- and F-region makes the problem of estimating E-region neutral winds substantially more difficult, and it is clearly leading to unreasonable results in the examples presented. Figure 10 shows the algorithm estimates non-zero neutral winds at 125-135 km altitude in a truth model simulation where the true neutral wind is zero. This behavior is pathological and unreasonable. The*

*results assert that the variance of the estimated electric fields at low altitudes is nearly infinitely large, when in reality electric field mapping should guarantee that electric fields at low altitudes should nearly match the fields at high altitudes.*

It is accurately noticed that we do not assume that the electric potential maps perfectly along the magnetic field. This allows our method to be used also in cases where this assumption can not be done.

The mapping of electric field along the magnetic field lines is not perfect. This is especially true on smaller scale structures or in the lower E region, as shown by Reid (1965) and Park and Dejnakintra (1974) (see also Brekke (2013)). This is also seen in Sangalli et al. (2009) where the electric field in the E region fluctuates.

The allowed variances for the electric field gradients is not considered in itself, but through Maxwells equations. However, there are no neighbouring voxels at the borders, which means that these gradients can not be implemented directly with differences between the neighbours. We thought about several techniques to handle this issue, which are shown in Figure 2 of the paper. Three of the techniques to handle the borders give border-crossing derivatives a larger uncertainty. This uncertainty is 20 mV/m per 2.5 km (1 m/s per km for neutral wind).

Also, as described in Section 4.3, the setup we use for the borders give the same uncertainty to gradients over the border as to those within the borders.

Apparently, our manuscript could be understood as we would use these constraints throughout the volume, possibly in all directions. We will try to clarify the manuscript.

4.-7.

We gratefully thank the referee for suggesting more reasonable strictnesses of the constraints we use. In general, those are stricter than those we use in our calculations. We performed new simulations using the constraints suggested by the referee in points 4-7 and letting the zeroth order Tikhonov regularization have an a priori standard deviation of 300 m/s. As a result, the electric field remains unchanged, but the neutral wind estimates become more varying and uncertain. To compare, we also tested how the model would react to the same situation if the wind blows with 300 m/s. Also here, the different strictnesses of regularization give small differences.

In general, one should not regularize an inverse problem more than necessary. Therefore the least strict assumptions are preferable because they then give more room for unforeseen variations in the ionosphere. We therefore do not want to tighten the constraints since it does not seem necessary. We will include these reasonings and references into the manuscript.

7.

*> The use of a zeroth-order Tikhonov regularization is going to bias the neutral wind estimates low. The assumed a priori variance is 200 m/s, but auroral neutral wind jets over 300 m/s have been observed, for example in the JETS rocket mission.*

It is correct that zeroth-order Tikhonov regularization biases the solution towards the a priori expected value, here zero. However, this bias is not as strong as the referee seems to suggest. The assumed standard deviation is 200 m/s - this means that winds of 300 m/s still would be at 1.5-sigma. A standard deviation for the wind components of 200 m/s would lead to a small under-estimate of these components of a few tens of metres per second.

## Minor comments

1.

> *The figure quality is generally low, with the text in the axis labels being highly pixelated.*

We will increase the figure resolution in the next version of the manuscript.

2.

> *An azimuth-elevation plot of the beam geometry would substantially clarify the beam geometry. Figures 3 and 4 have so many lines on them that the 3D geometry is hard to see.*

We will include a plot showing the azimuth-elevation distribution of transmit beams.

3.

> *Lines 209 and 210 should specify the interpulse period assumed for this experiment and specify how many independent estimates of the ACF/Spectra are obtained in 2 s of integration.*

We will include this information to the manuscript

## References

Brekke, Asgeir (2013): Physics of the upper polar atmosphere. 2. edition, Springer, Heidelberg.

Park, C. G. and Dejnakintra, M. (1974): Paper presented at Fifth International Conference on Atmospheric Electricity, Garmisch-Partenkirchen, West Germany, September 2–7, 1974.

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Sangalli, L., D. J. Knudsen, M. F. Larsen, T. Zhan, R. F. Pfaff, and D. Rowland (2009): Rocket-based measurements of ion velocity, neutral wind, and electric field in the collisional transition region of the auroral ionosphere, Journal of Geophysical Research: Space Physics, vol. 114 number A4, doi: 10.1029/2008JA013757.

Please also note the supplement to this comment:

<https://angeo.copernicus.org/preprints/angeo-2022-11/angeo-2022-11-AC2-supplement.zip>